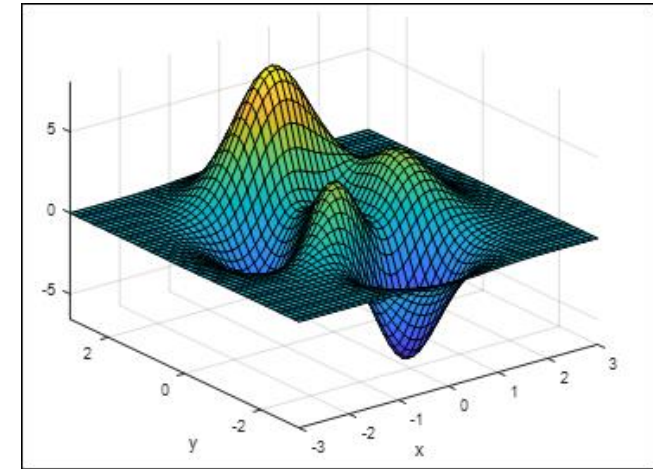
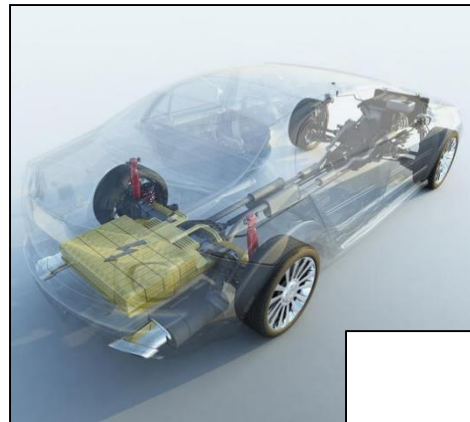


# Objective Drivability Calibration

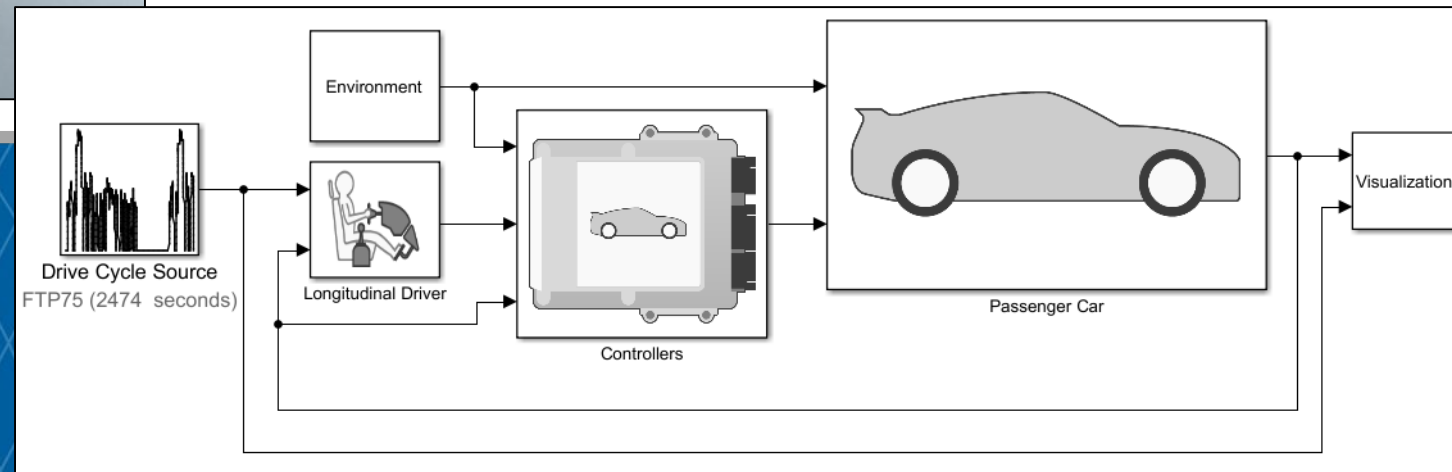
MathWorks Automotive  
Conference

April 30<sup>th</sup>, 2019



Co-Authors:  
Jason Rodgers\* &  
Jan Janse van Rensburg

MathWorks

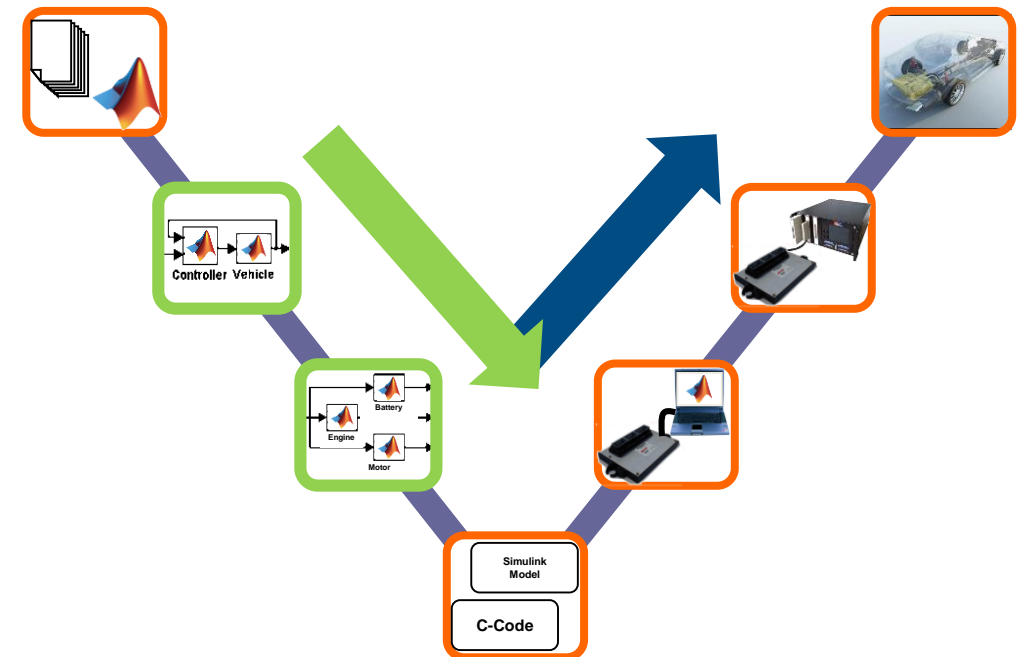
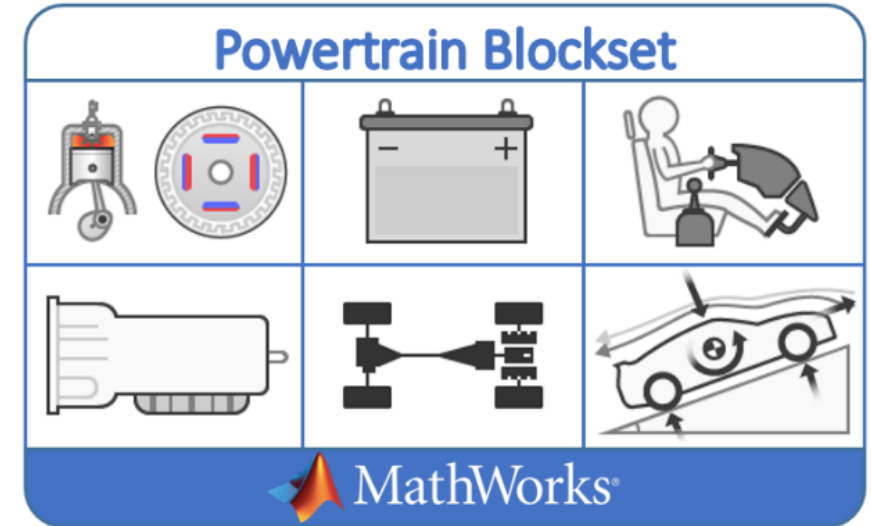


# Presenter

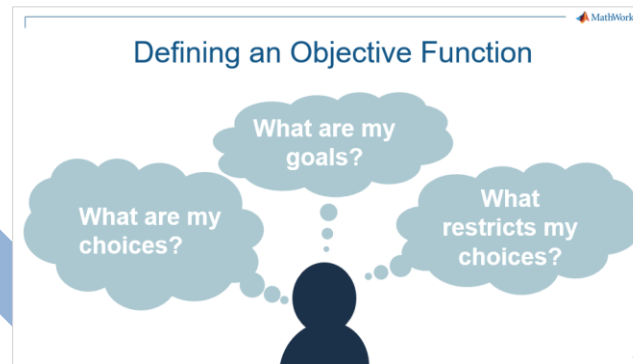
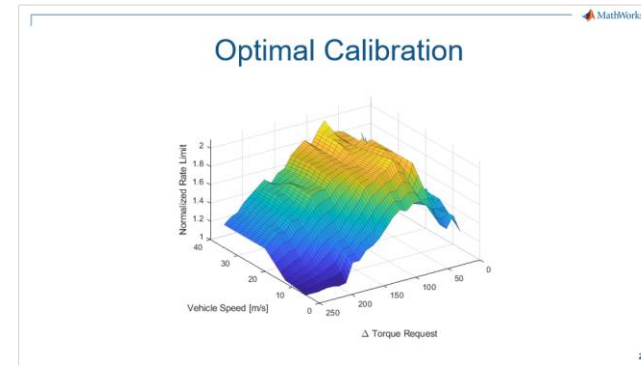
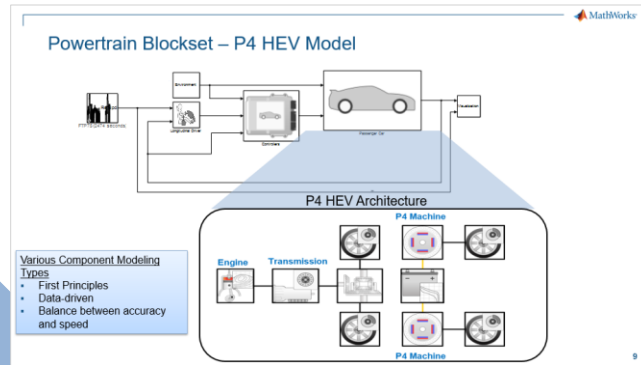
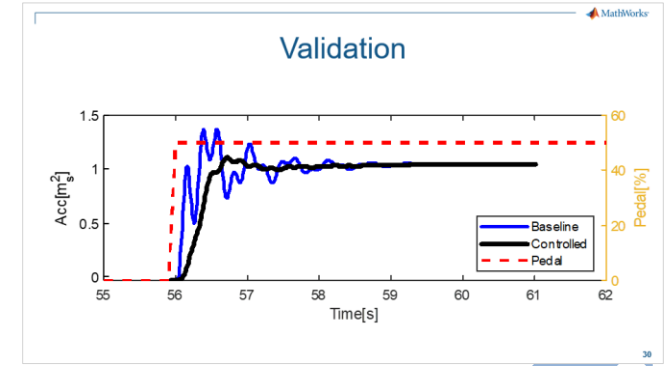
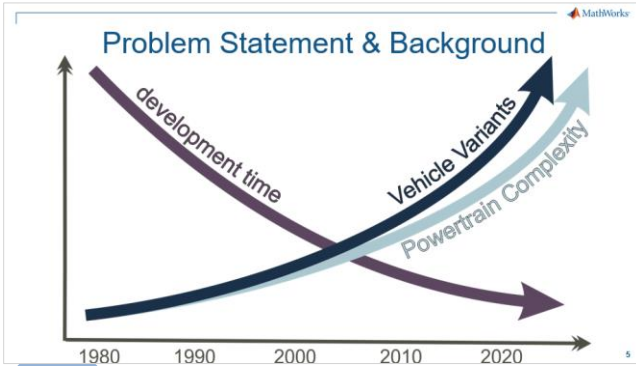
- Jason Rodgers
  - MathWorks Senior Application Engineer
    - Vehicle Dynamics Blockset
    - Powertrain Blockset
    - Model Based Calibration Toolbox
  - Previous experience at Toyota R&D
    - System Optimization and Control engineer
    - Optimizing powertrain design and controls subject to various constraints (cost, FE, drivability, etc.)
  - Education
    - BSME and MSME, University of Michigan
  - Areas of interest
    - Enabling Model-Based Design using physical modeling
    - Applying optimization techniques to modeling and control problems
    - Applying new technologies such as Deep Learning to Automotive problems

# Key Takeaways

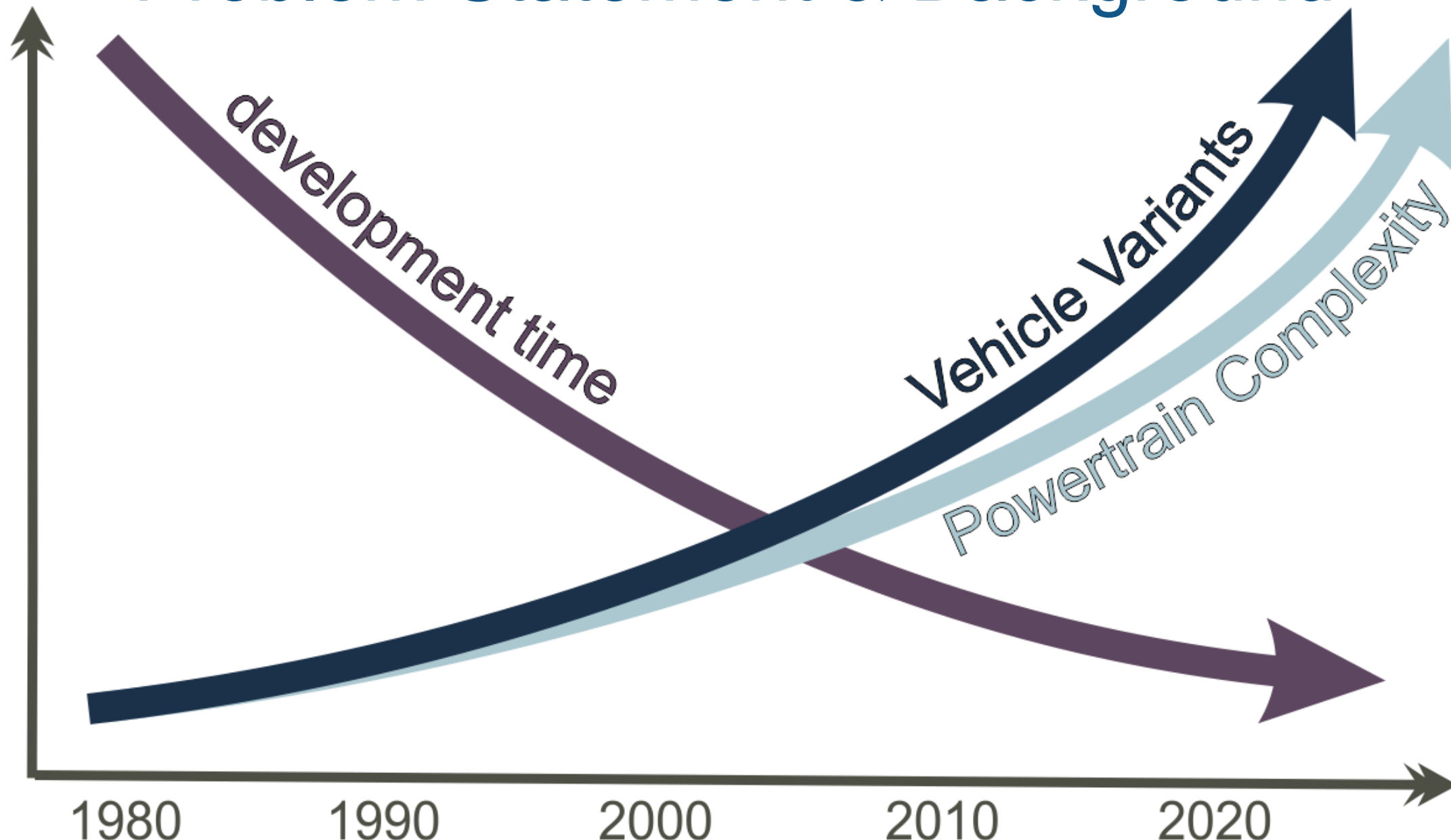
- Powertrain Blockset is capable of simulating low frequency **drivability** behavior
  
- **Model re-use** from early planning phase can be used to jumpstart **calibration** efforts
  
- Objective-based calibration can:
  - **Improve** calibration time
  - Account for performance **trade-offs**
  - Trace back to **requirements**
  - **Objective** and not subjective → **repeatable**



# Agenda

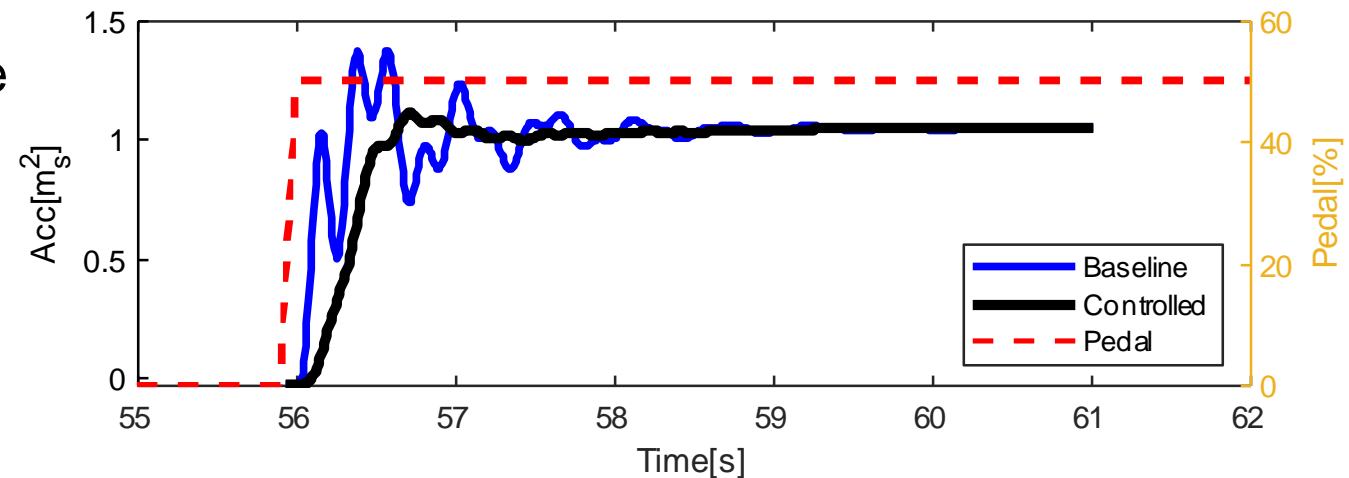
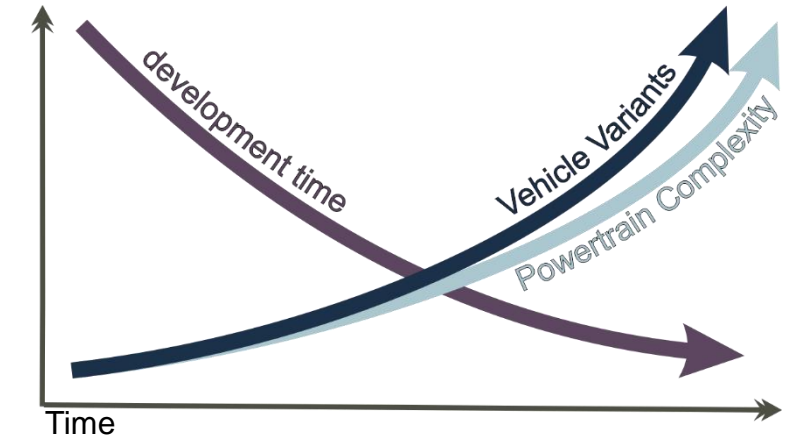


# Problem Statement & Background



# Problem Statement

- What is the problem?
  - ECU can have dramatic effect on drivability
  - Manual calibration is time sink
  - Ratings are defined by experienced but subjective drivers
  - Efficiency improvements are needed
    - Decreasing development time
    - Increasing powertrain complexity and number of variants
- How to solve the problem?
  - Use objective based approach to tune ECU calibration parameters
    - I. Requirements driven
    - II. Objective based - Repeatable
    - III. Automated – Time savings
    - IV. Optimal with respect to requirements



# Background

## What is drivability?

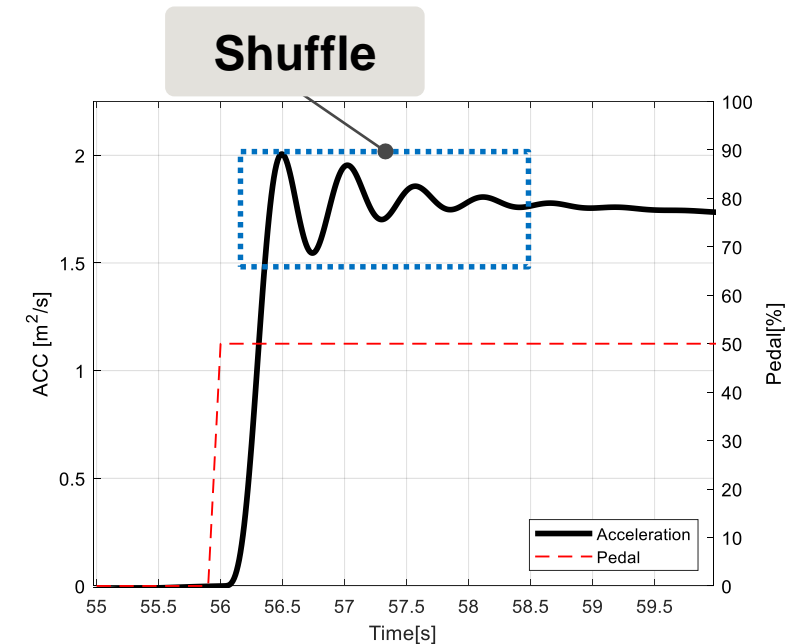
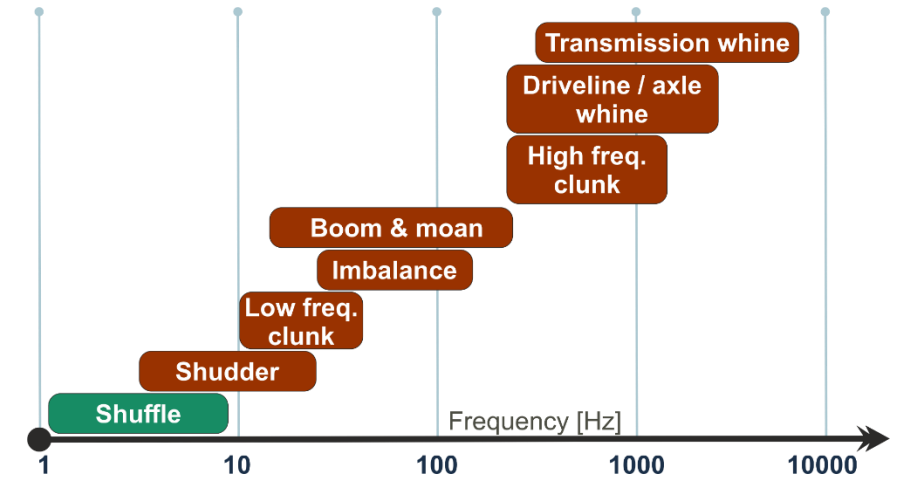
- Response characteristic of the vehicle to driver inputs under different driving conditions
- Want the driver to be as comfortable as possible
  - Hesitation
  - Sluggish
  - Hard start
  - Noise/Oscillations
- Drivability is affected by many sources
  - Gear shifts
  - Engine Idle
  - Braking
  - Acceleration
  - Etc.



# Background

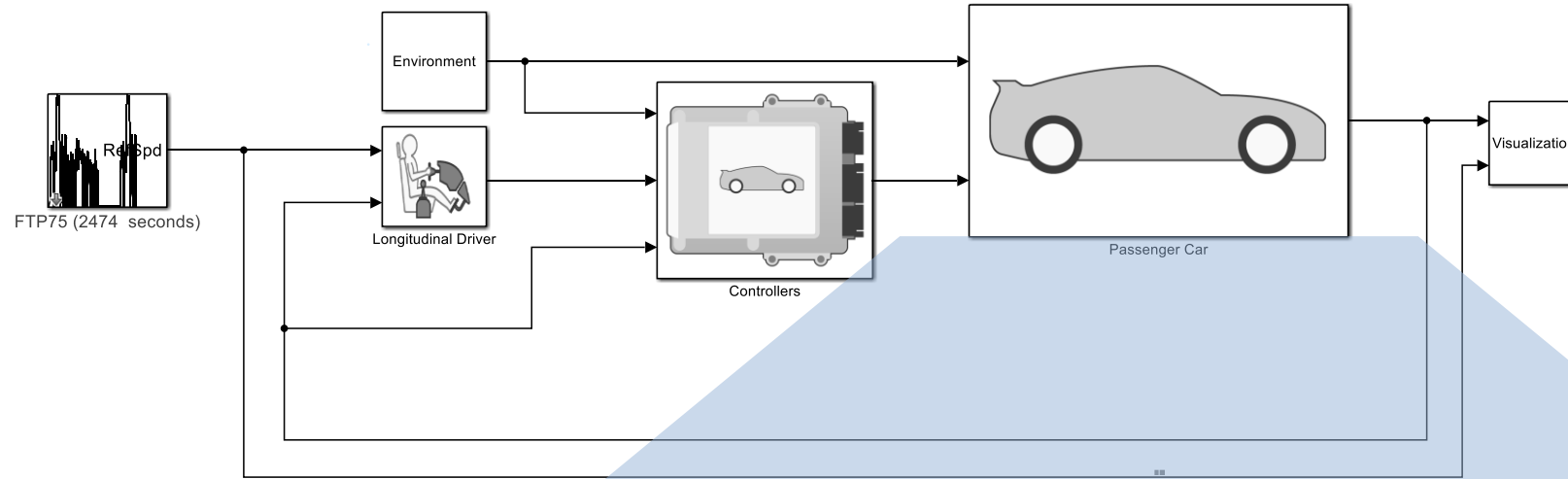
## What are we focusing on?

- Shuffle related to tip in
  - NVH longitudinal effect caused by sudden changes in the drive torque
  - Some room to optimize hardware but controller is more cost effective
  - 2-8 Hz depending on the gear
- Not considering shift shock, clunk, or higher order modes
- Acceleration is measured at CG
- No gear shift during tip in event

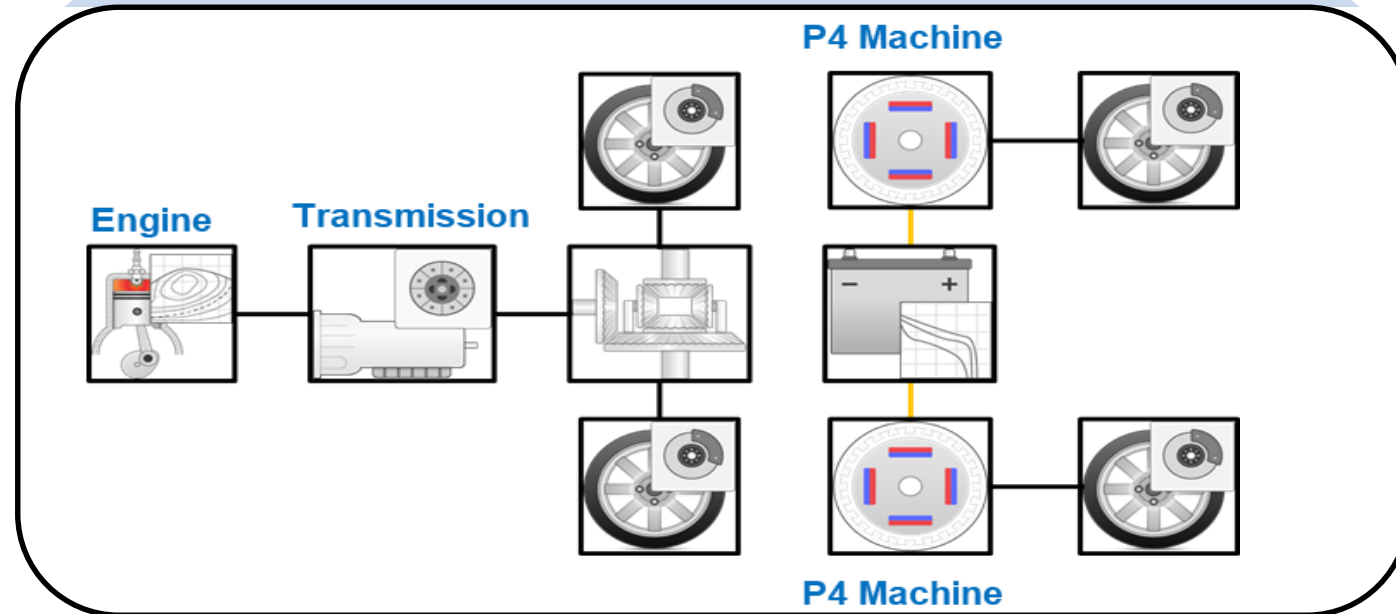




# Powertrain Blockset – P4 HEV Model



## P4 HEV Architecture

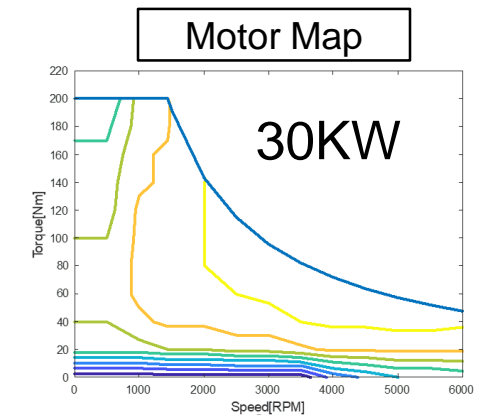
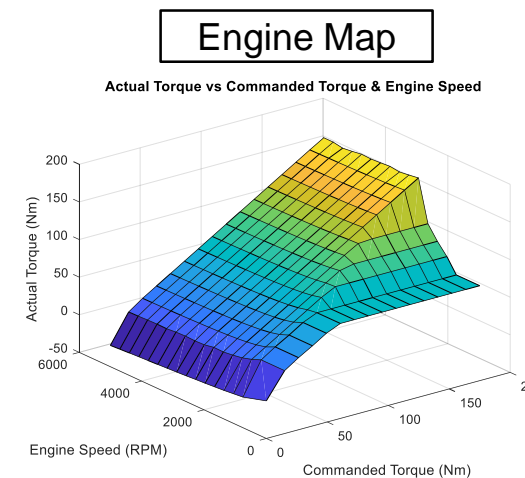
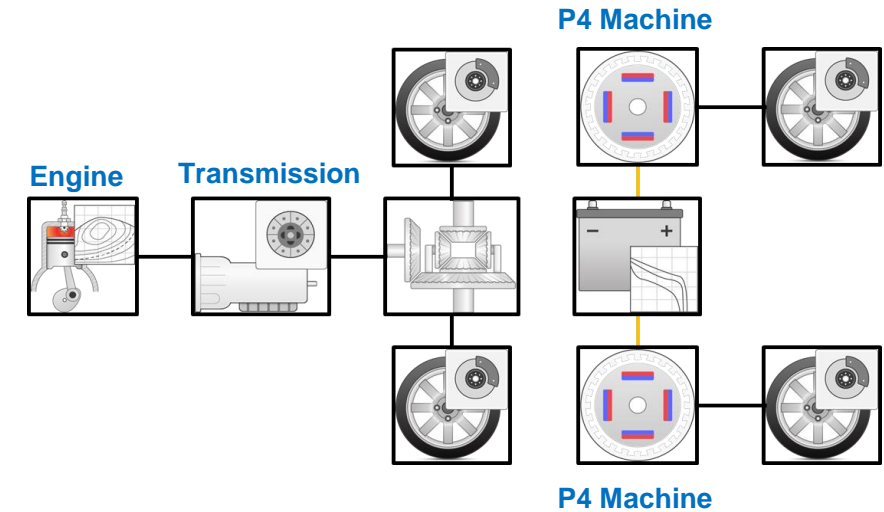


### Various Component Modeling Types

- First Principles
- Data-driven
- Balance between accuracy and speed

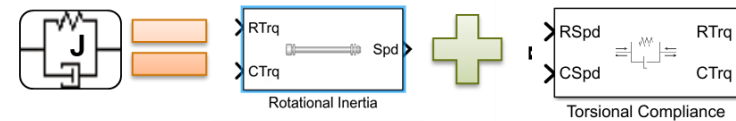
# Powertrain Blockset – P4 HEV Model

- P4 HEV Powertrain model
  - Started from reference application and modified for testing and added tip-in controller
  - Model fidelity is typical for Fuel Economy and acceleration studies
  - Model reuse
- Engine
  - 1.5L L4 95kW(126hp) @5500RPM
  - Map-Based Model
- 2 P4 30kW Motors
  - Map-Based Model
- 1.3 kWh Battery
  - Map-Based Model



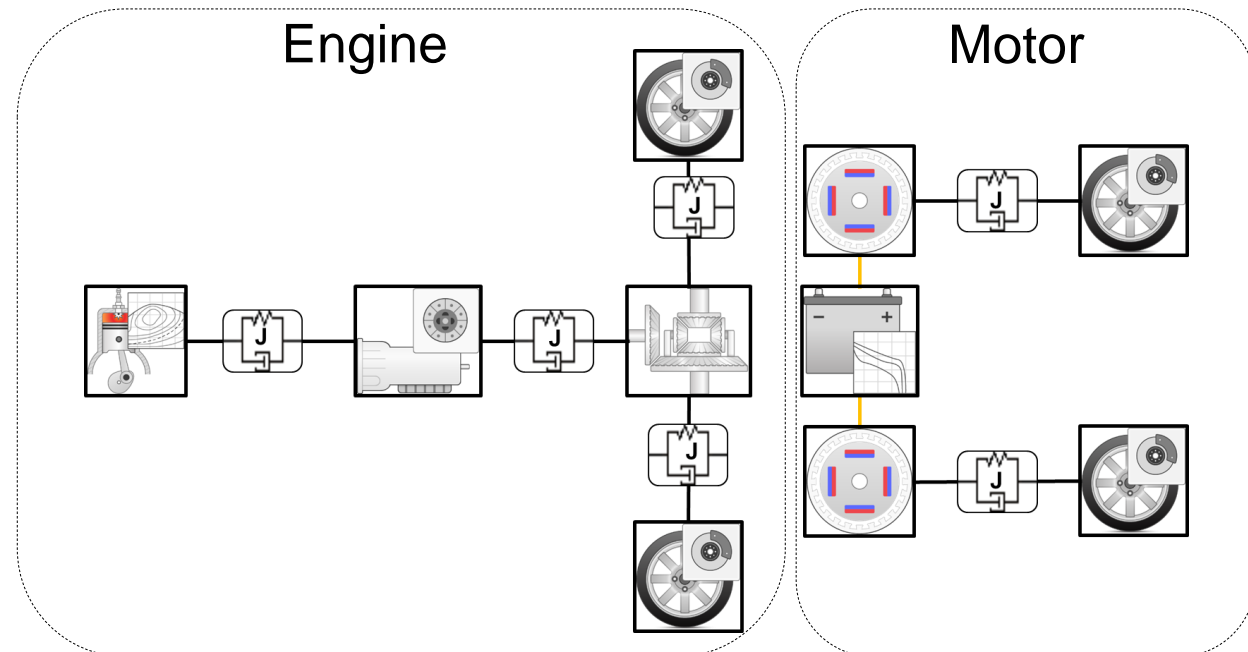
# P4 Component Modeling

- Driveline oscillations are captured by rotational inertia and compliance blocks that exist in reference model



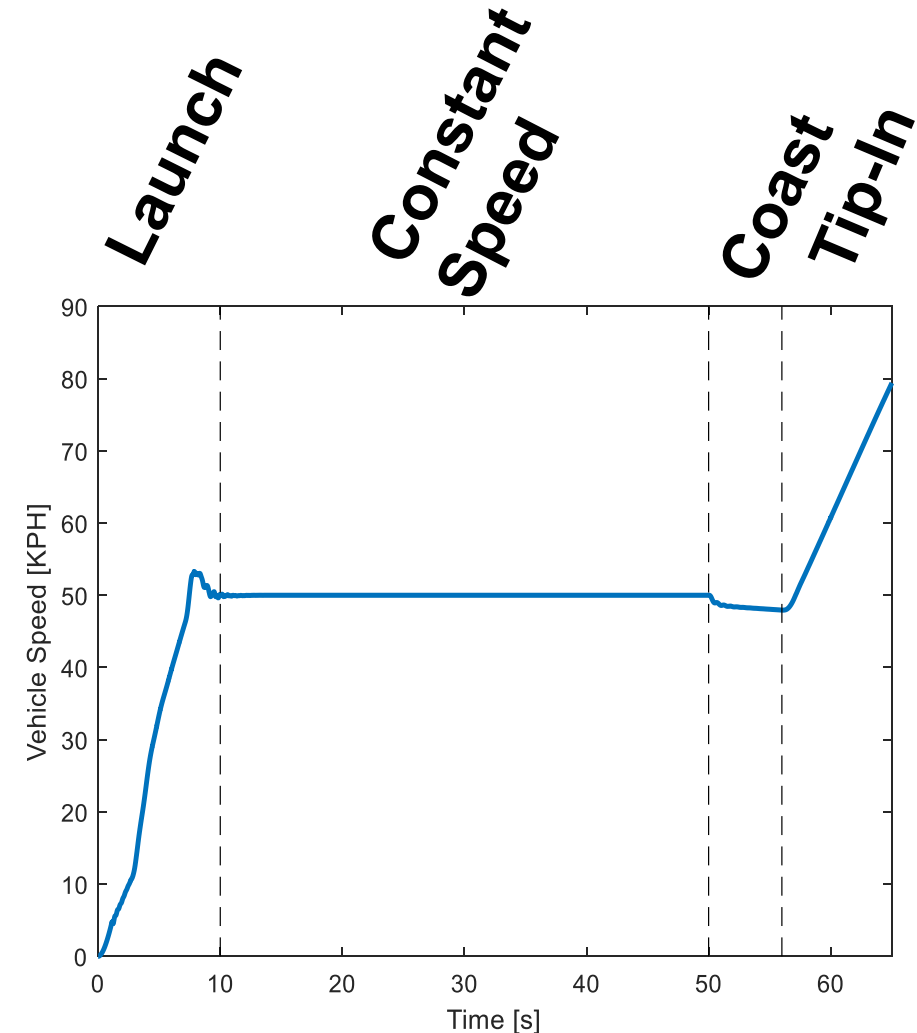
- Linear damping and stiffness
  - Openness of model allows for replacing with nonlinear components

- 2 Torque Paths
  - Engine
  - Motor



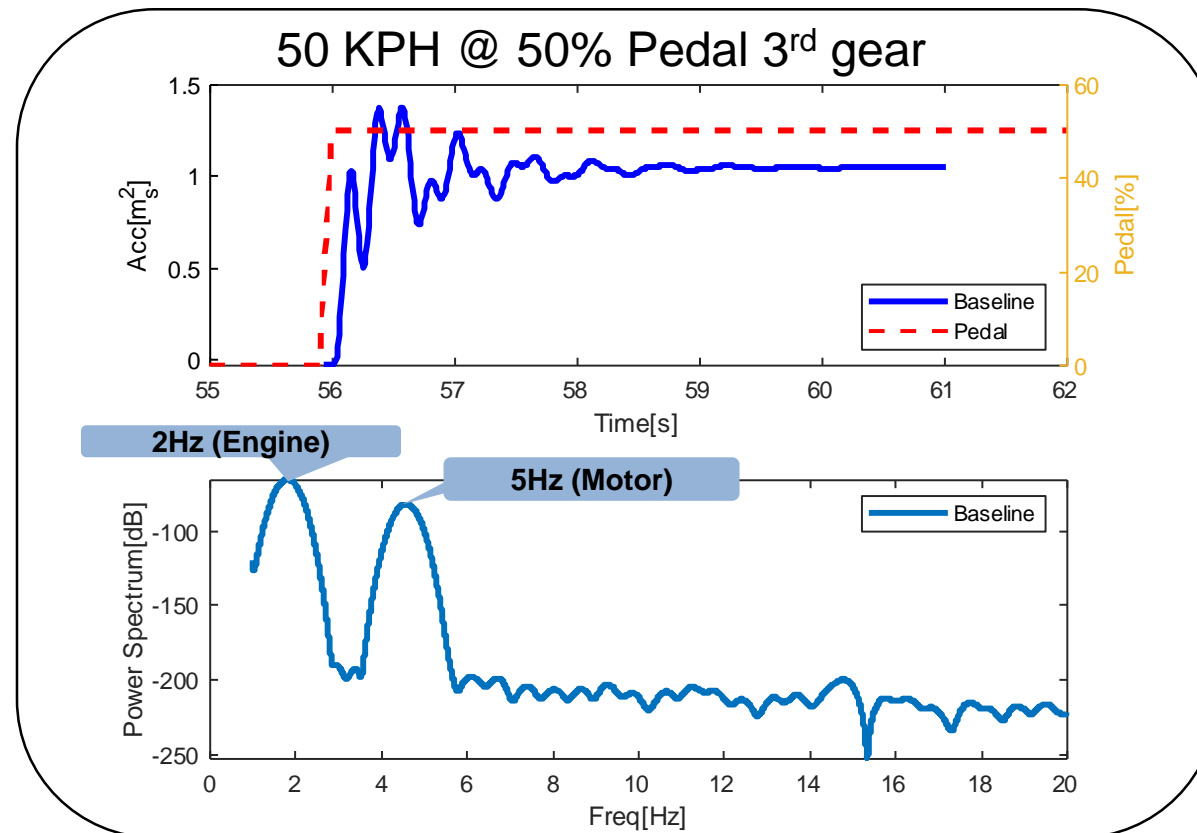
# Driving Scenario

- What scenario are we using?
  - Accelerate to Constant Speed
  - Hold Speed and shift to desired gear. Allow transients to subside.
  - Let off pedal
  - Apply pedal step input



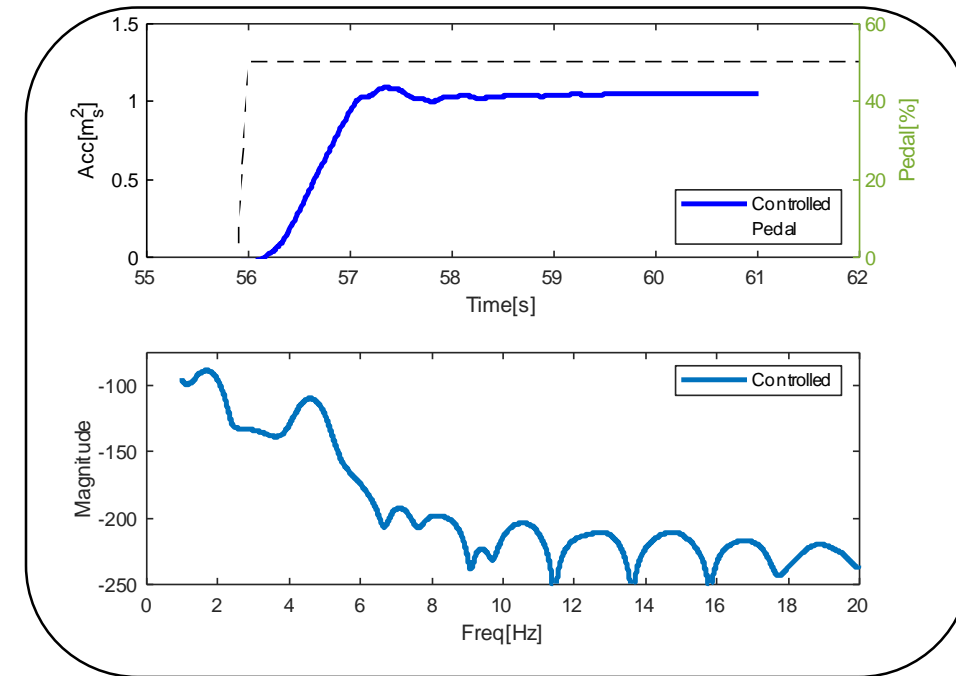
# Tip-In Acceleration Response

- Initial response has large amounts of shuffle oscillations
  - Model is able to capture the first mode (shuffle) for both torque paths
  - Response attenuation is required to improve drivability



## Tip-In Acceleration Response

- How to improve?
  - Spark Control (on engine side only)
  - Fixed **Rate-Limit** on torque request or pedal input
  - Scheduled **Rate-Limit**
  - Optimal Control – e.g. Model Predictive Control



Example: Manually Calibrated Rate Limit

### First Pass at Improvements:

- Reduced oscillations but response is slow
- Is a function of gear, speed, and torque request → scheduled rate-limit
- Long manual process to do by hand (weeks)
- How to balance responsiveness and oscillations?

**Define an Objective Function and Optimize!**

# Defining an Objective Function



What are my choices?

What are my goals?

What restricts my choices?

# Optimization Introduction

- **Objective function** – What you are trying to achieve?
  - Minimize measured signal
- **Design variables** – What parameters need to be adjusted?
  - Physical model parameters
  - Controller gains
- **Constraints** – What are the bounds or constraints of the design variables?
  - Min/Max values
  - Can handle inside objective function

*Minimizing (or maximizing) objective function(s) subject to a set of constraints*

## Objective Function

$$\min_x f(x)$$

Linear or nonlinear

Design variables  
(discrete or continuous)

### Linear constraints

$$Ax \leq b$$

$$A_{eq}x = b_{eq}$$

$$l \leq x \leq u$$

### Nonlinear constraints

$$c(x) \leq 0$$

$$c_{eq}(x) = 0$$



# Formulating an Optimization Problem for Objective Drivability

## Variables

What are my choices?

- Rate limit
  - Gear
  - $\Delta$ Torque Request
  - Vehicle speed

## Objective

What are my goals?

- Minimize oscillations
- Minimize response time

## Constraints

What restricts my choices?

- Response Time
- Jerk
- Etc.

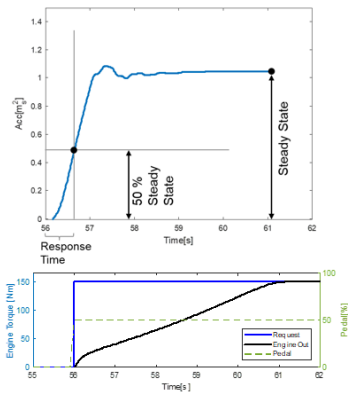
# Objective Function

## Shuffle Objective Function

$$\min_{RL} (t_{resp} + jerk_{max} + VDV + constraints)$$

### Cost Function Metrics

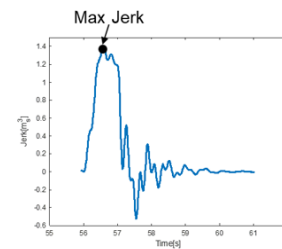
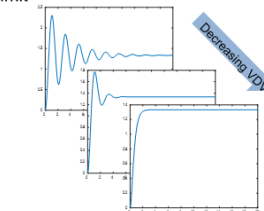
- Response Time
  - $t_{resp}$  = time to reach 50% steady state acceleration
  - Normalized by the slowest desired response time (1s)
  - Defined this way to account for edge cases where motor or engine cannot provide enough torque



Example: Low engine speed with high torque request

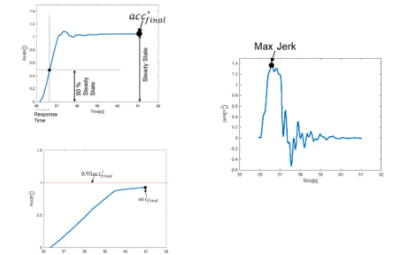
### Objective Function Metrics

- Vibration Dose Value (VDV)
  - $VDV = \left( \int_0^T a^4(t) dt \right)^{1/4}$
  - VDV is sensitive to the peaks in the acceleration.
  - Normed to the maximum response with no rate limit
- Maximum Jerk
  - $jerk_{max} = \max \left( \frac{da}{dt} \right)$
  - Normed to the maximum jerk obtained with no rate limit



### Objective Function Constraints

- Response Time  $\leq 1$ sec
- Maximum Jerk  $\leq 2 \frac{m}{s^3}$
- $acc_{final} \geq 0.95 acc_{final}^*$ 
  - $acc_{final}^*$  is the steady state acceleration with no rate limit
  - useful for edge cases
- Barrier Method used for constraint handling
  - $constraints = \begin{cases} 10^6 & \text{if violated} \\ 0 & \text{otherwise} \end{cases}$

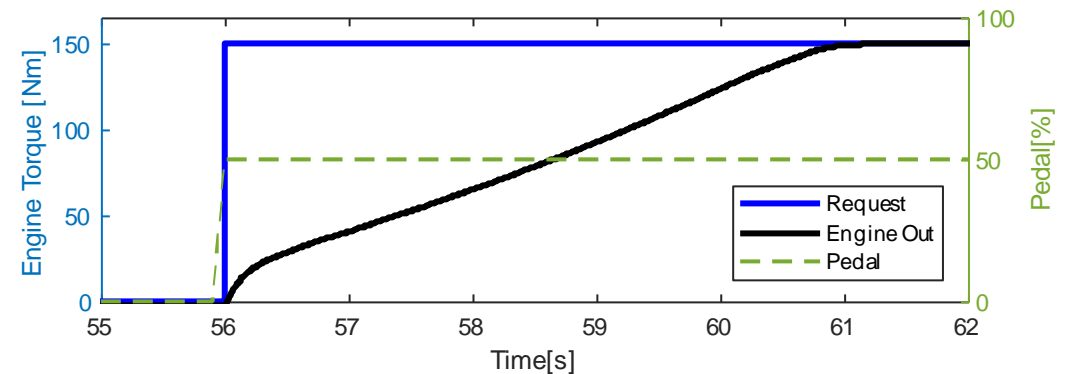
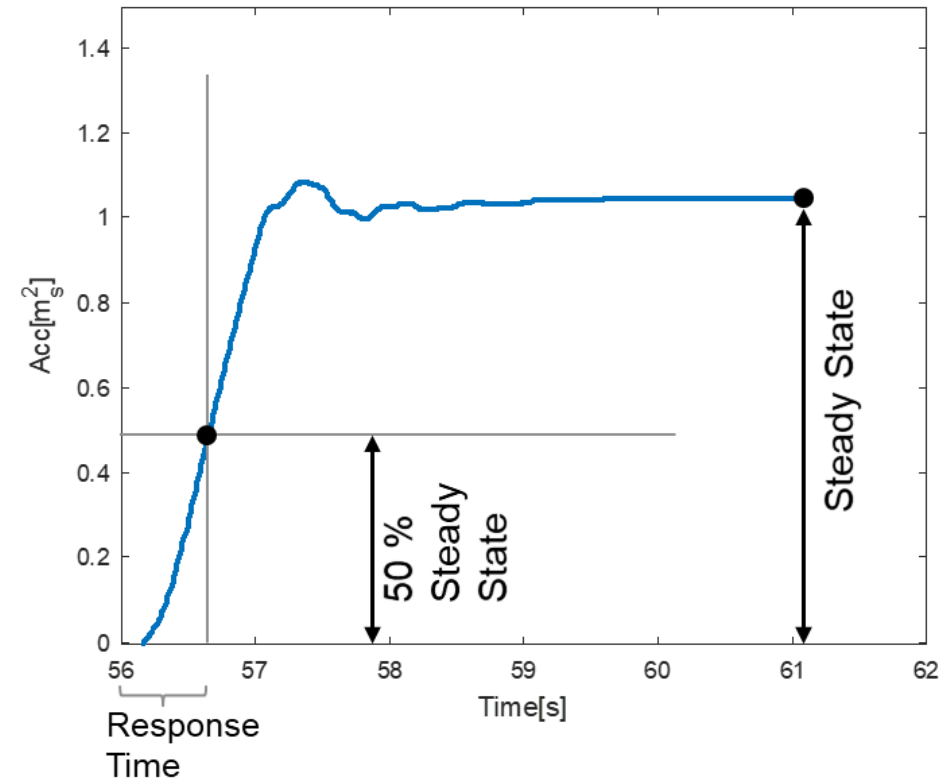
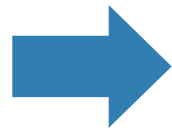


Constraints  $\Rightarrow$  Requirements

# Cost Function Metrics

- Response Time
  - $t_{resp}$  = time to reach 50% steady state acceleration
  - Normalized by the slowest desired response time (1s)
  - Defined this way to account for edge cases where motor or engine cannot provide enough torque

Example: Low engine speed with high torque request

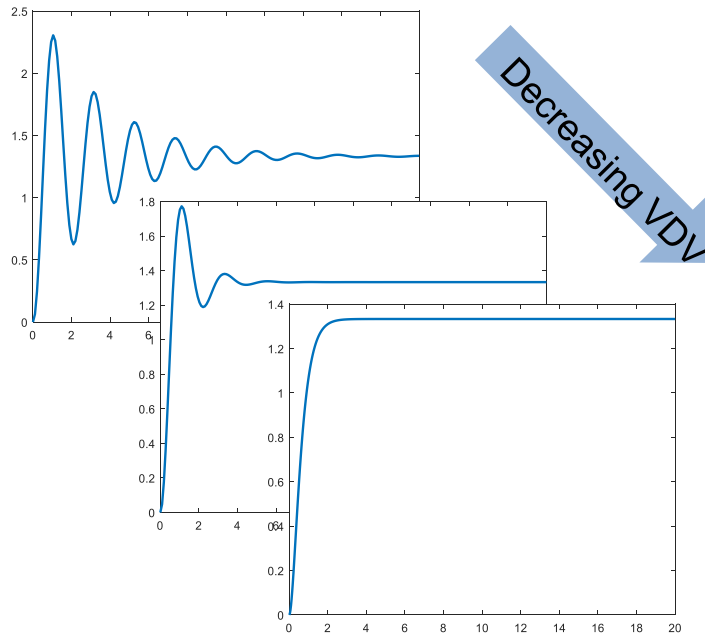


# Objective Function Metrics

- Vibration Dose Value (VDV)

$$VDV = \left( \int_0^T a^4(t) dt \right)^{1/4}$$

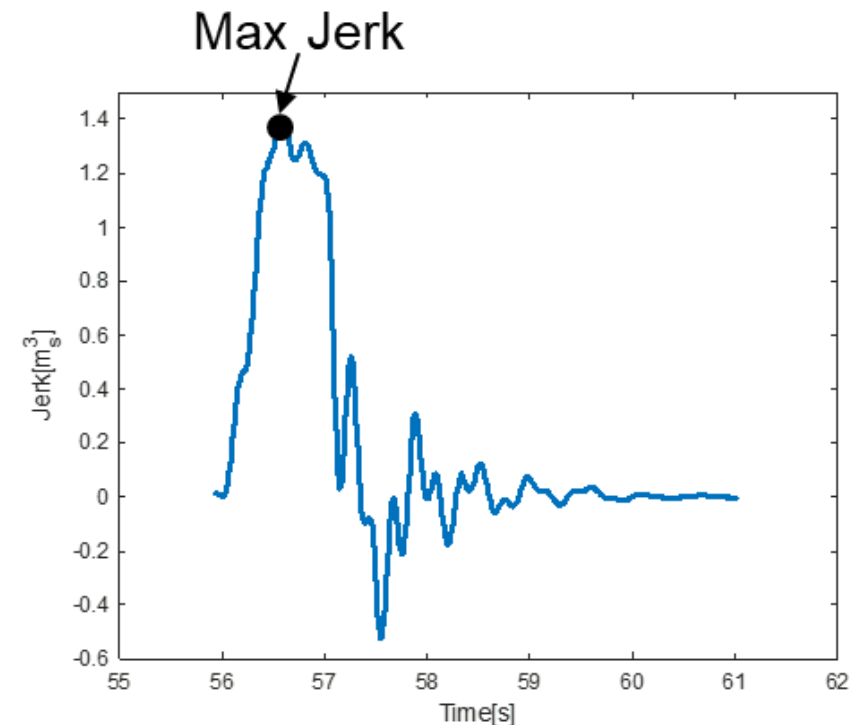
- VDV is sensitive to the peaks in the acceleration.
- Normed to the maximum response with no rate limit



- Maximum Jerk

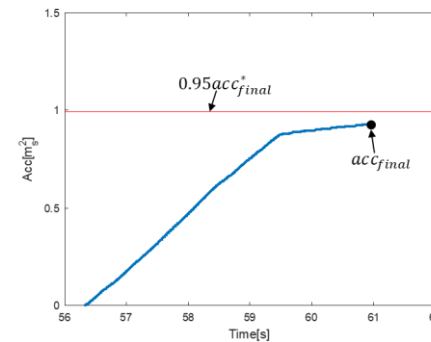
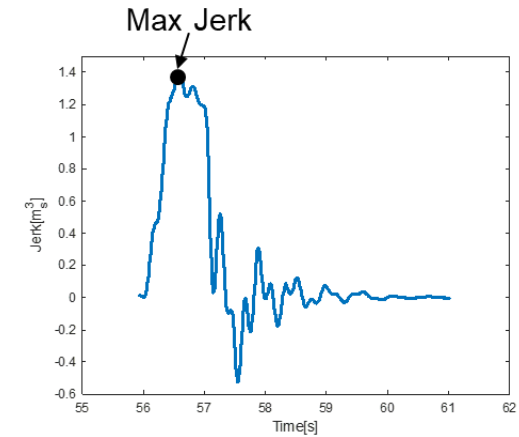
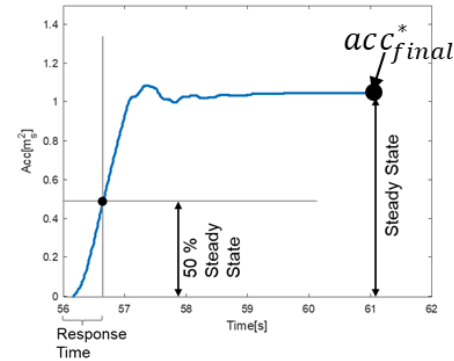
$$jerk_{max} = \max \left( \frac{da}{dt} \right)$$

- Normed to the maximum jerk obtained with no rate limit



# Objective Function Constraints

- Response Time  $\leq 1$ sec
- Maximum Jerk  $\leq 2 \frac{m}{s^3}$
- $acc_{final} \geq 0.95 acc_{final}^*$ 
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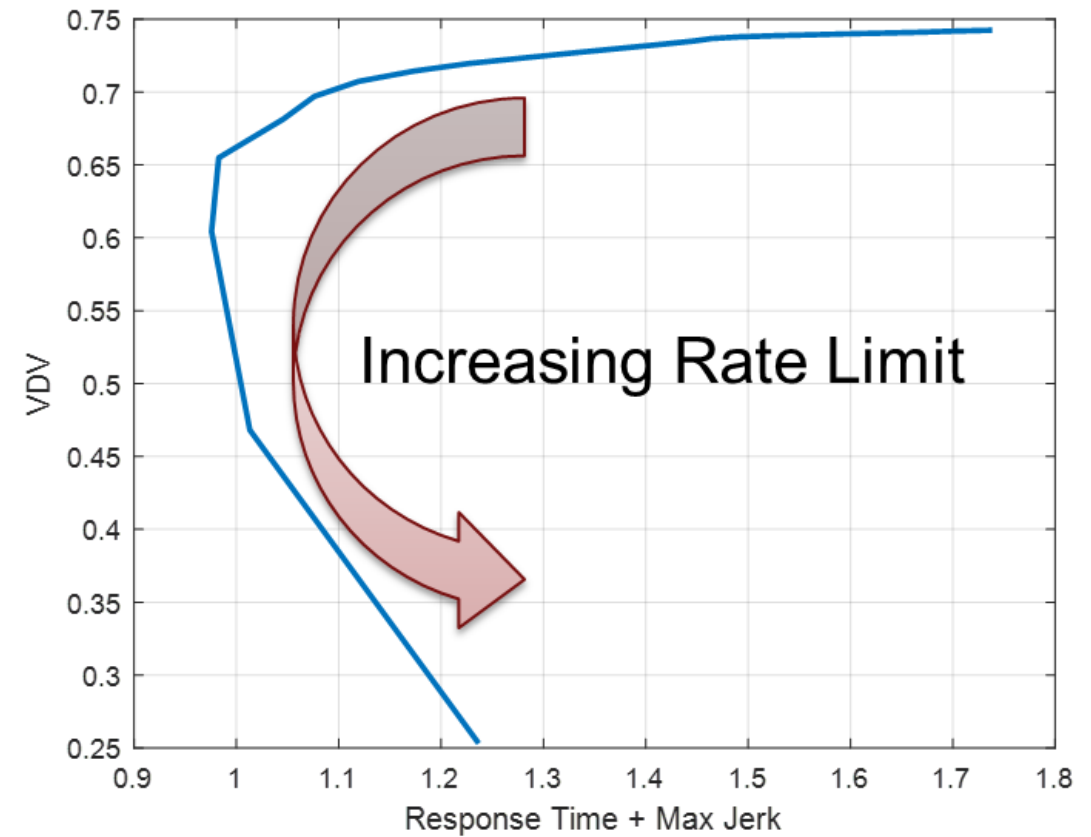


**Constraints  $\Rightarrow$  Requirements**

# Objective Function

## Observations

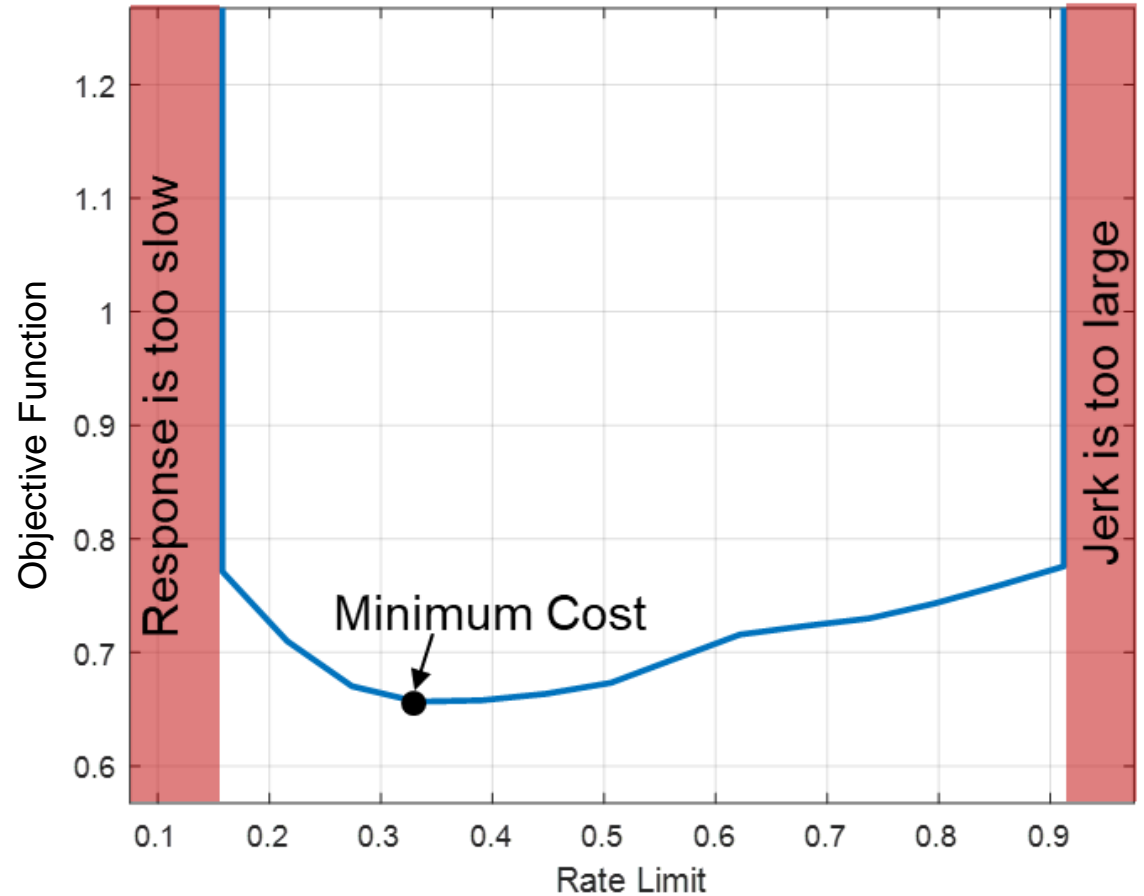
- Pareto curve exists between oscillations and response time
  - the faster the response, the more oscillations



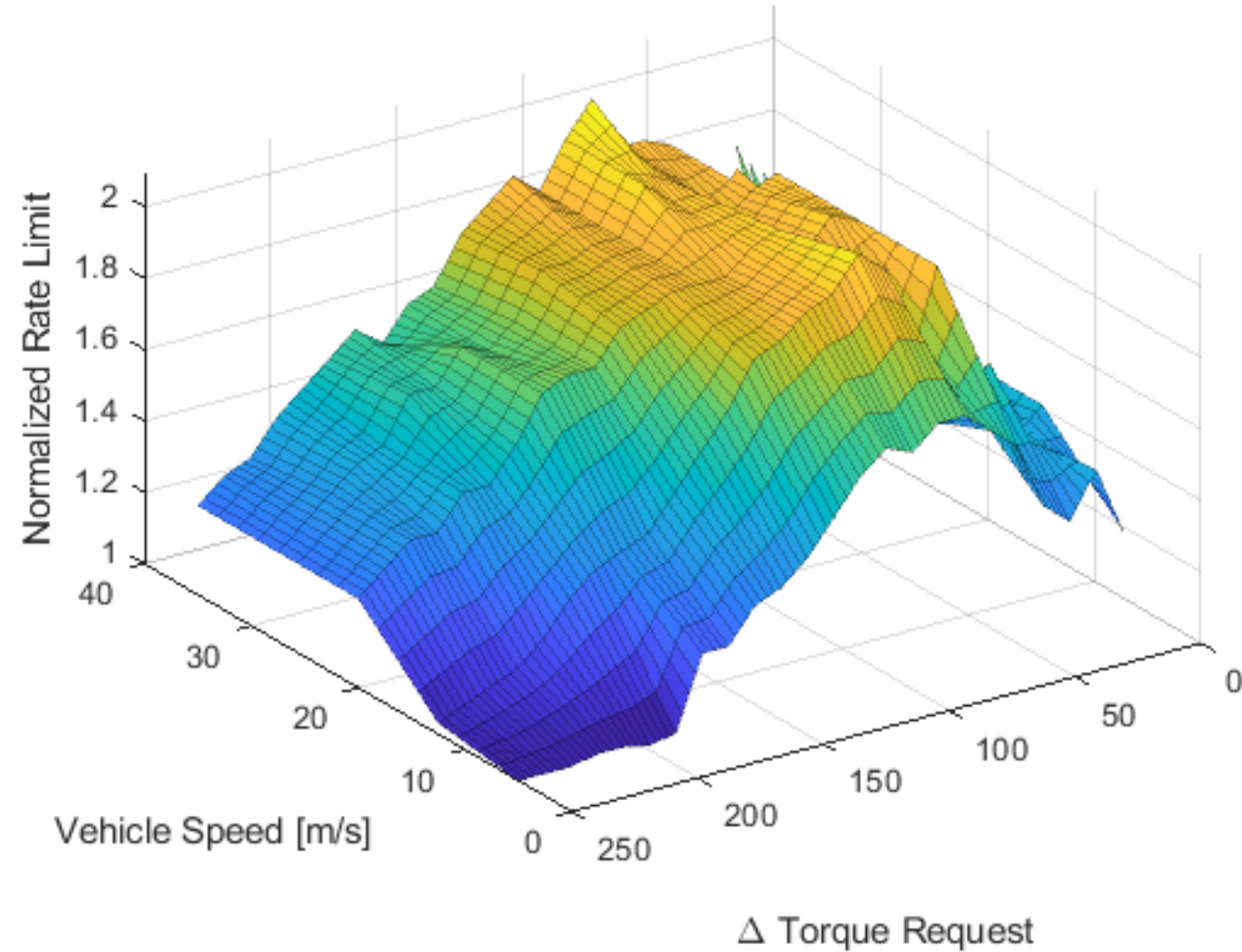
# Objective Function

## Observations

- Objective function:
  - Can be non-smooth
  - Can have multiple minima



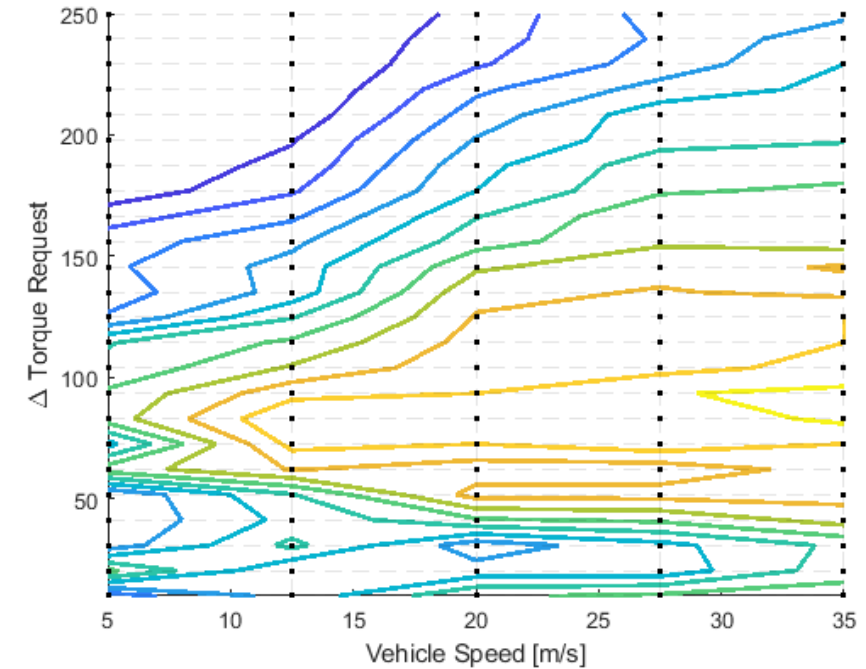
# Optimal Calibration





# Calibration Process

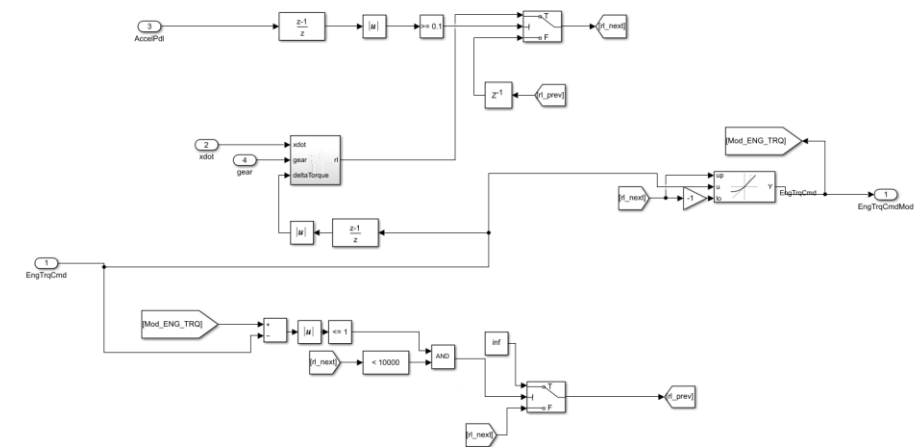
- Intel Xeon E5 processor – 3.6GHz, 6 cores
- 64GB RAM
- 1806 Optimal Rate-Limits
  - 7 total maps (6 for engine, 1 for motor)
  - 24  $\Delta$ torque breakpoints
  - 5 speed breakpoints
  
- Traditionally, this process could take days or **weeks** for **manual calibration**
- **10 hours** to **automatically** calibrate using pattern search global optimization algorithm



Search Algorithm	Time	Solution Found
fmincon	1.5minutes	✘
Particle Swarm	5 minutes	✔ +
Pattern Search	1.5minutes	✔

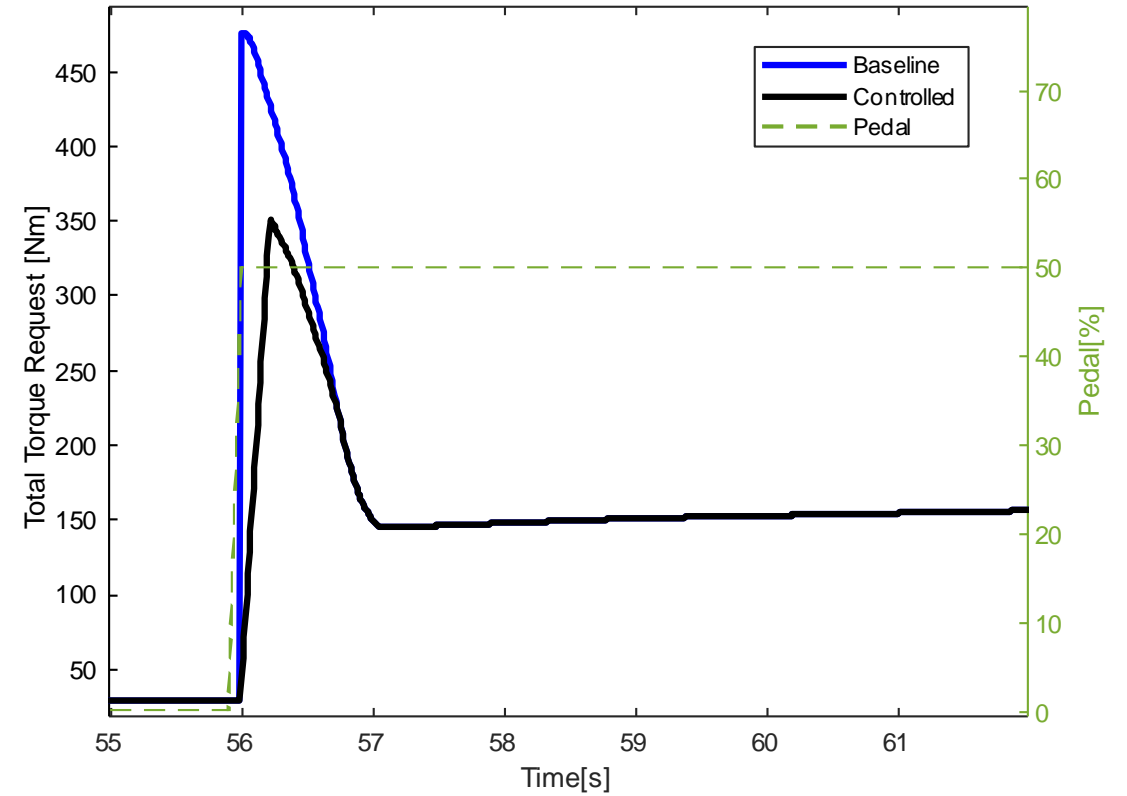
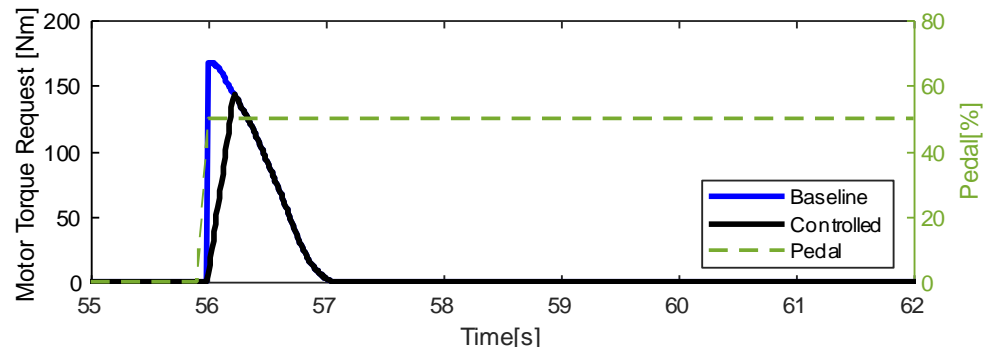
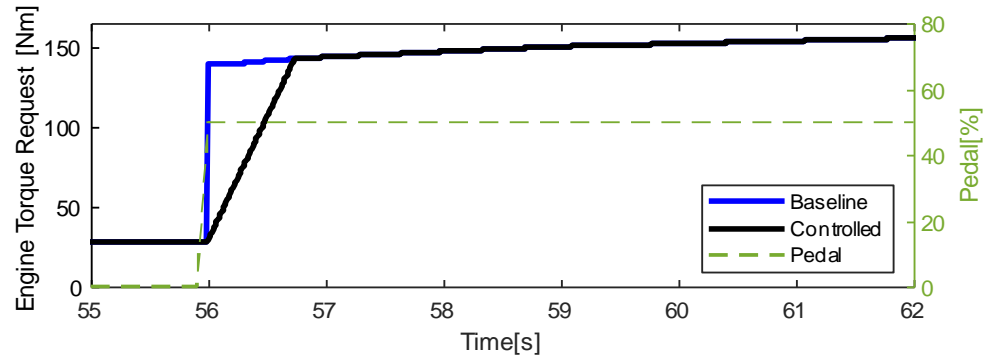
# Tip-In Controller

- Rate limit is calculated as a function of  $|\Delta\text{Torque request}|$ , vehicle speed, and Gear (engine side only)
- Rate limit is applied when judged a tip in response
  - $|\Delta\text{Torque request}| > 10\text{Nm}$
  - Vehicle Speed  $> 2\text{ MPH}$
- Rate limit held until modified torque is near final desired torque value.



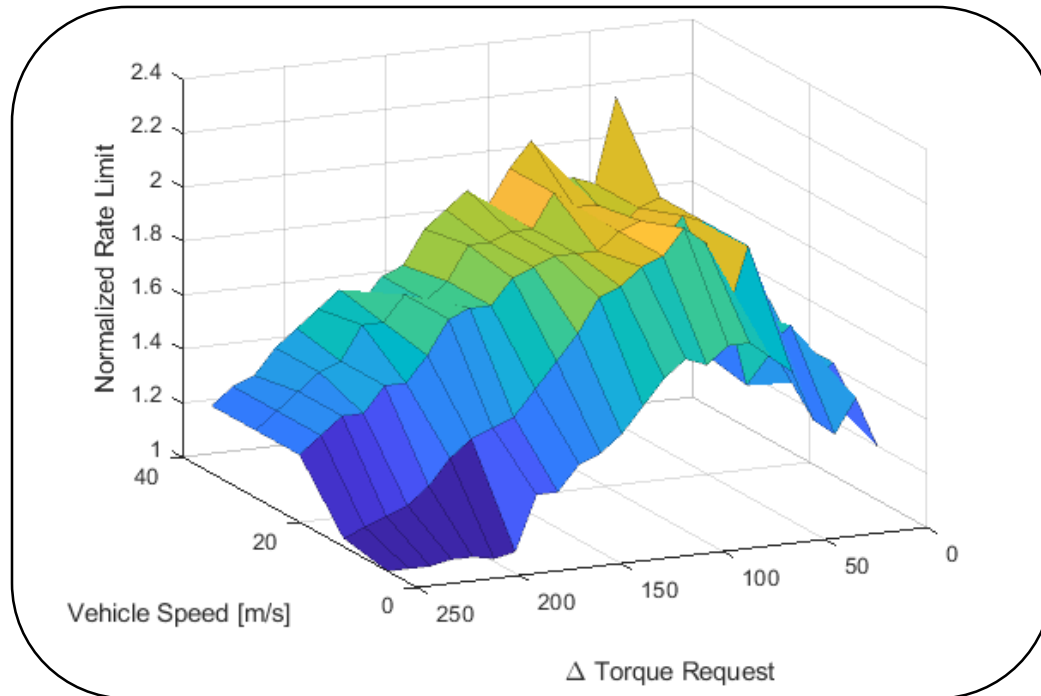
# Tip-In Controller

- Controlled Response

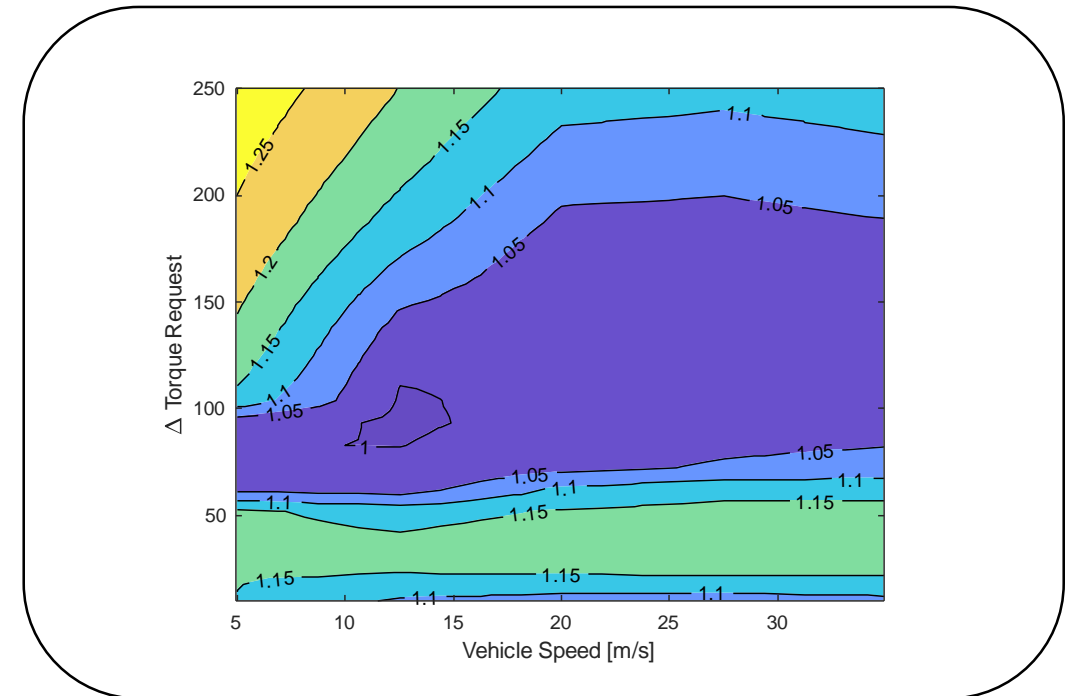


# Calibration Tables

- Areas of high sensitivity in the objective function can be used to redefine map breakpoints
- Example results for 5<sup>th</sup> gear

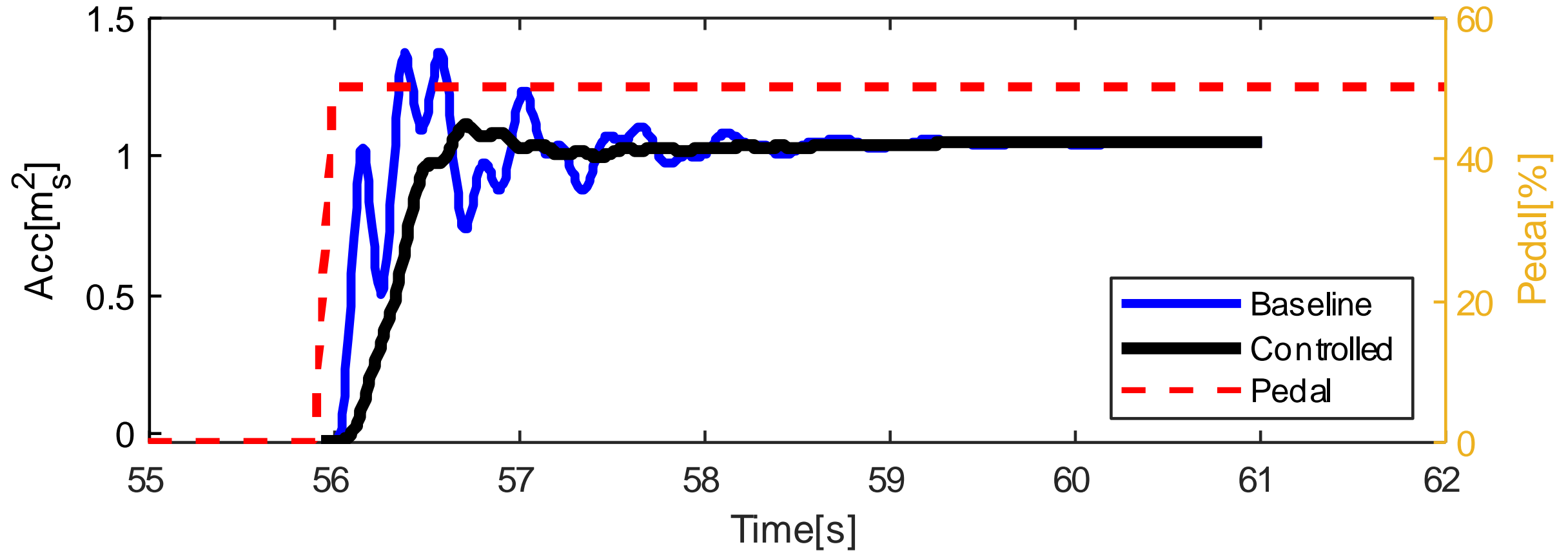


Calibration Map



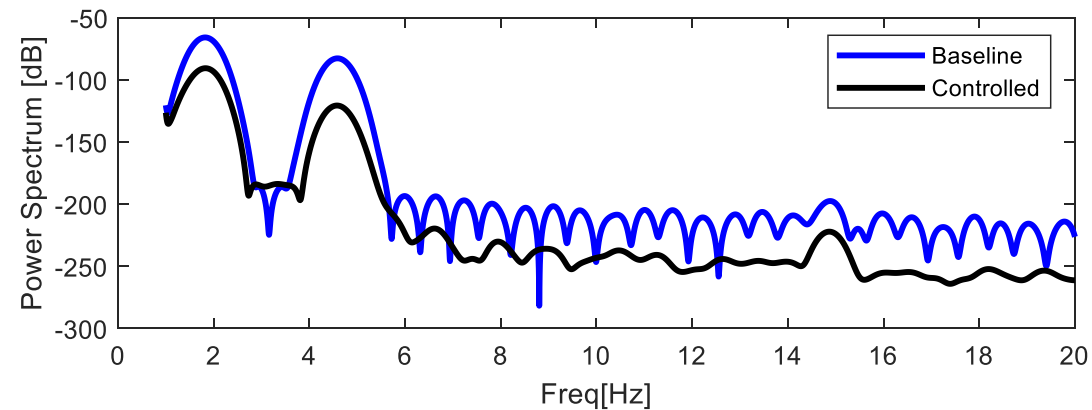
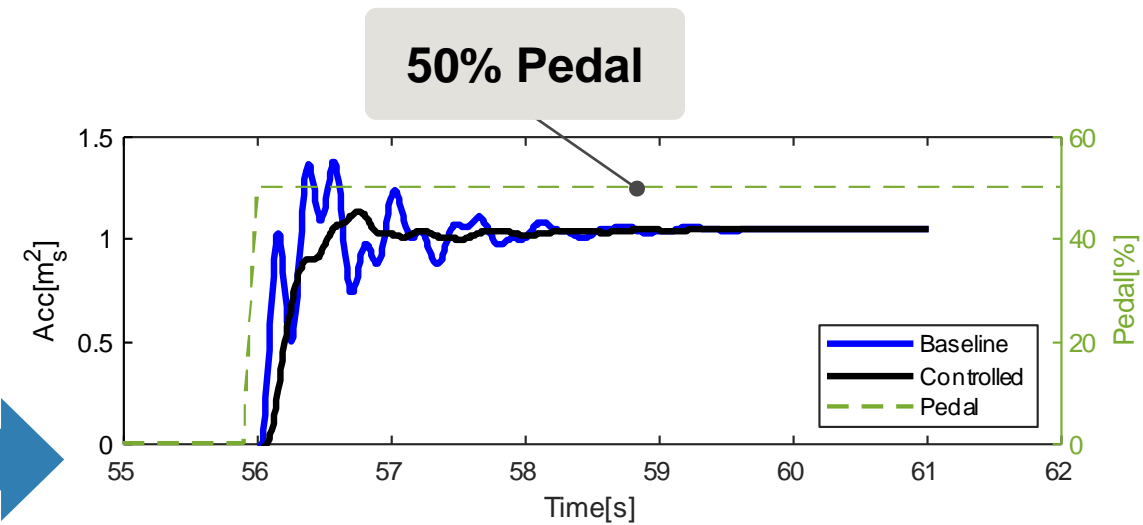
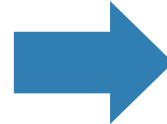
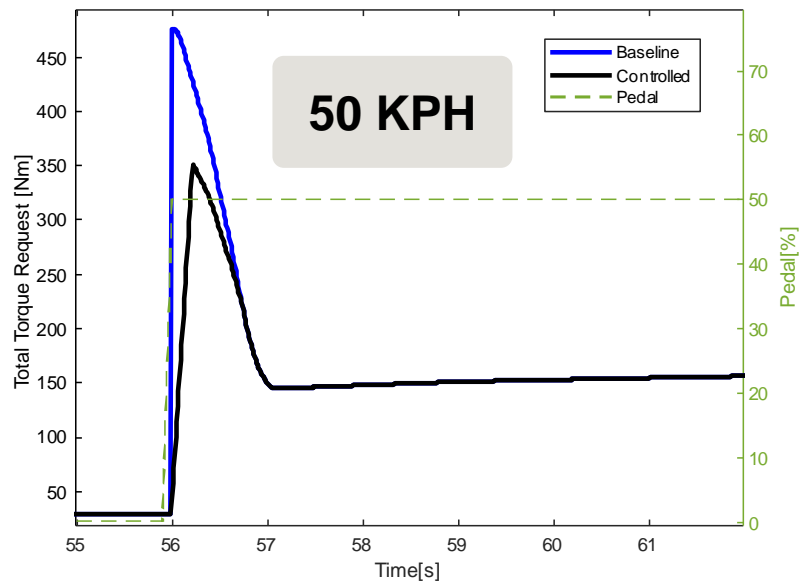
Optimized Objective Function Values

# Validation



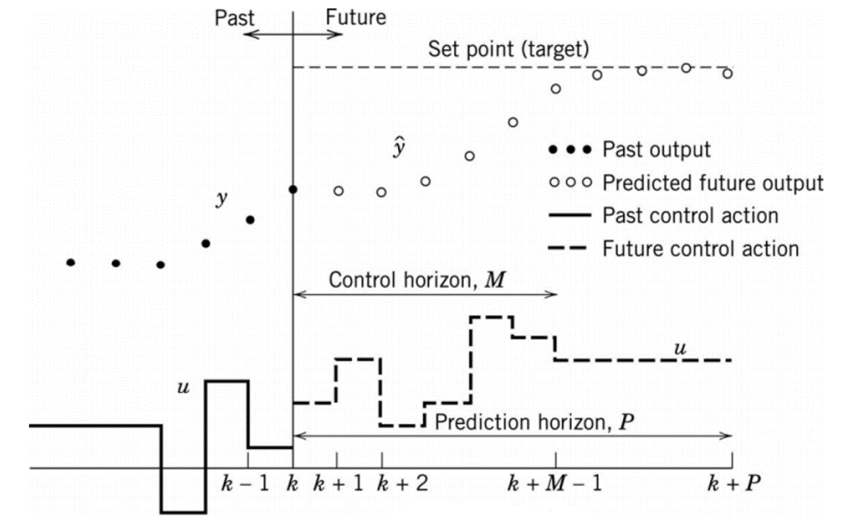
# Tip-In Results

- First engine and motor modes have decreased greatly (~50dB)
- Fast Tip-In response – 0.5s

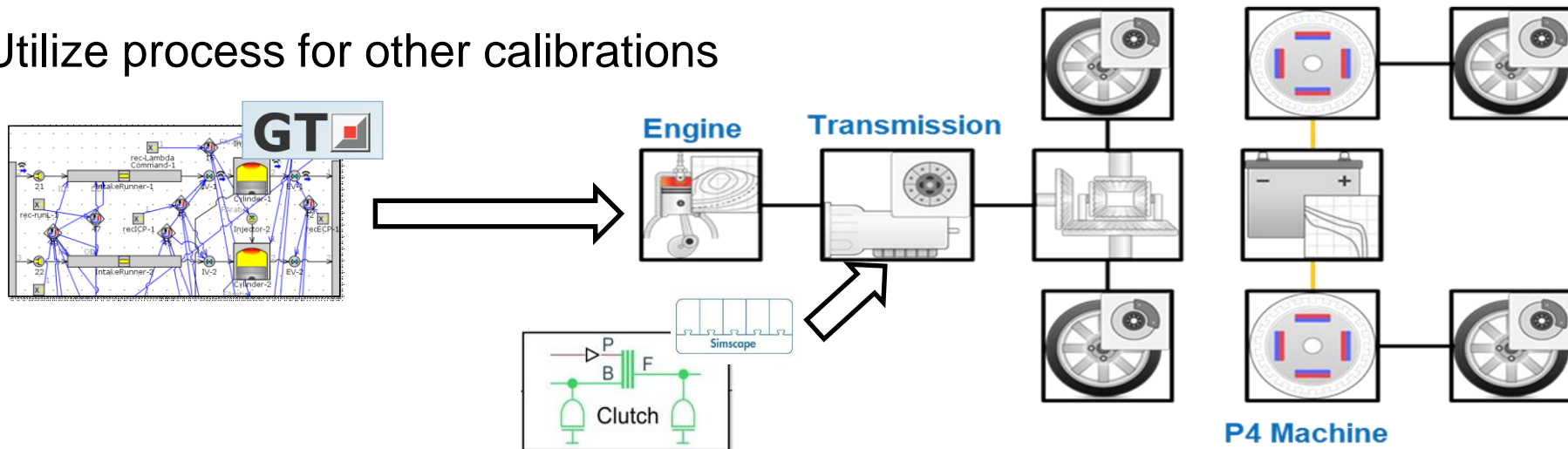


# Next Steps

- What are possible next steps?
  - Investigate more control options
    - Use sensitivity analysis to refine breakpoints in calibrated maps
    - Model Predictive Control with consideration for Fuel Economy
  - Process can be reused as model fidelity increases
    - GT Engine model
    - Simscape Driveline

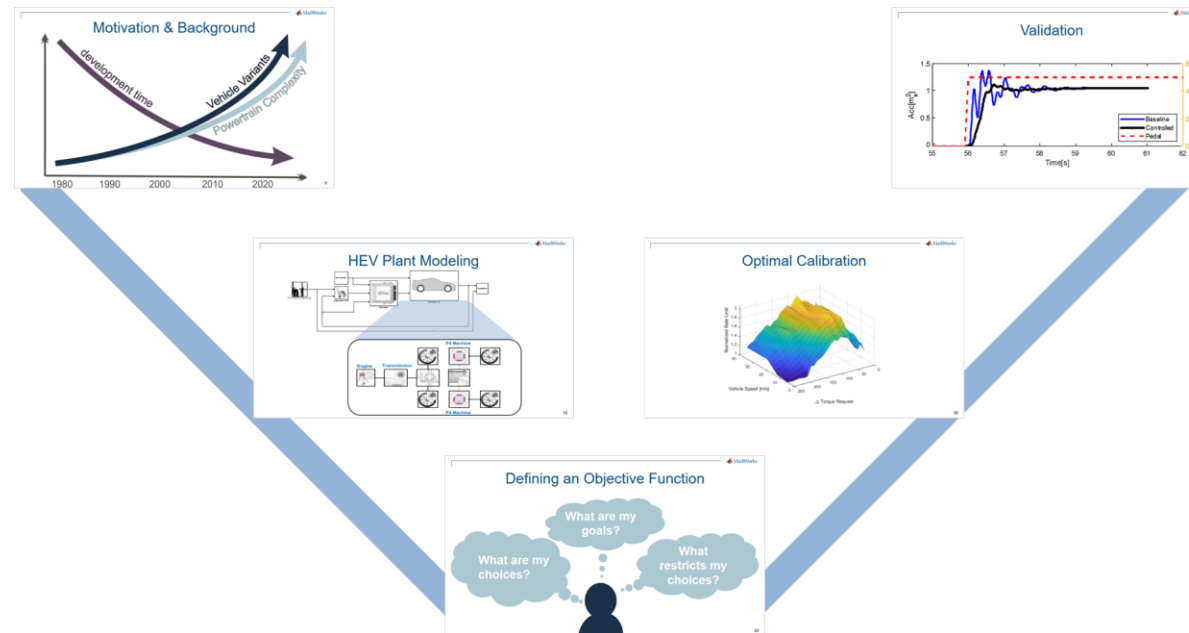


- Utilize process for other calibrations



# Summary

- A process for using an objective function to automate and improve shuffle response was shown
- Virtual calibration allowed process to be done in hours instead of weeks
- Along with FE and Acceleration characteristics, can also start to consider some drivability metrics during early phase planning





# Thank You



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Senior Application Engineer  
[jrogers@mathworks.com](mailto:jrogers@mathworks.com)

# References

Wellmann, T., Govindswamy, K., Braun, E., and Wolff, K., "Aspects of Driveline Integration for Optimized Vehicle NVH Characteristics," SAE Technical Paper 2007-01-2246, 2007

Atabay, O., Ötkür, M., & M Ereke, İ. (2018). Model based predictive engine torque control for improved drivability. *Proceedings of the Institution of Mechanical Engineers, Part D: Journal of Automobile Engineering*, 232(12), 1654–1666. <https://doi.org/10.1177/0954407017733867>

Jauch, C.; Tamilarasan, S.; Bovee, K.; Guvenc, L.; Rizzoni, G. Modeling for drivability and drivability improving control of HEV. *Control Eng. Pract.* 2018, 70, 50–62.  
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Wei, X., & Rizzoni, G. (2004). Objective metrics of fuel economy, performance and driveability—A review. *SAE Technical Paper*, 2004(2004-01-1338), <http://dx.doi.org/10.4271/2004-01-1338>.