

# Determining Vibro-Acoustic Effects in Multidomain Systems using a Custom Simscape Gear Library

Tim Dackermann, Rolando Dölling

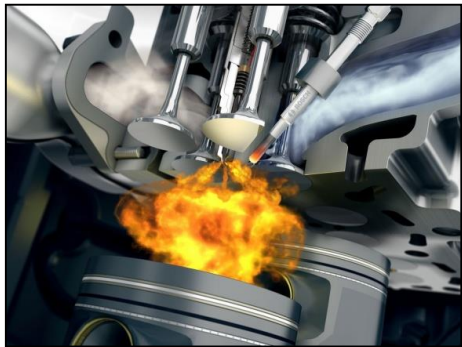
Robert Bosch GmbH

Lars Hedrich

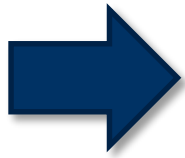
Goethe-University Ffm



# Power transmission



Combustion engine



...



Gearing



...



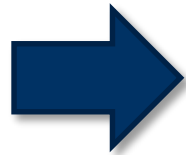
Tires & vehicle

Pictures: [1]

# Noise emission



Electric motor



...



Gearing



...



Tires & vehicle

Pictures: [1]

# Noise emission

Goal 1

Goal 2

Goal 3



Analysis

Optimization

Prediction

**Multidomain System  
Modeling**

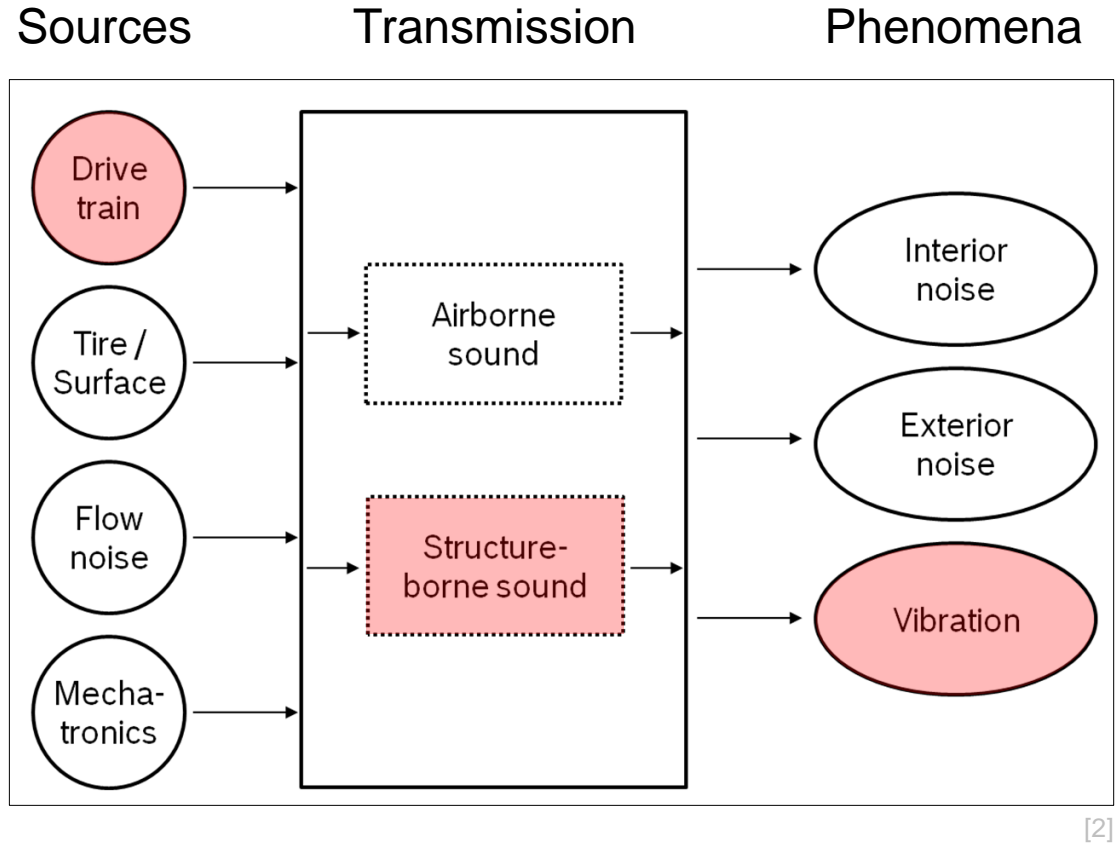
## Outline

- Vibro-acoustic sources and transmission paths
- Requirements for a vibro-acoustic gear model
- Mechanical excitation mechanisms
- **Flexible gear model library in SimMechanics**
  - Idea and concept
  - Implementation
  - Application
- Conclusions



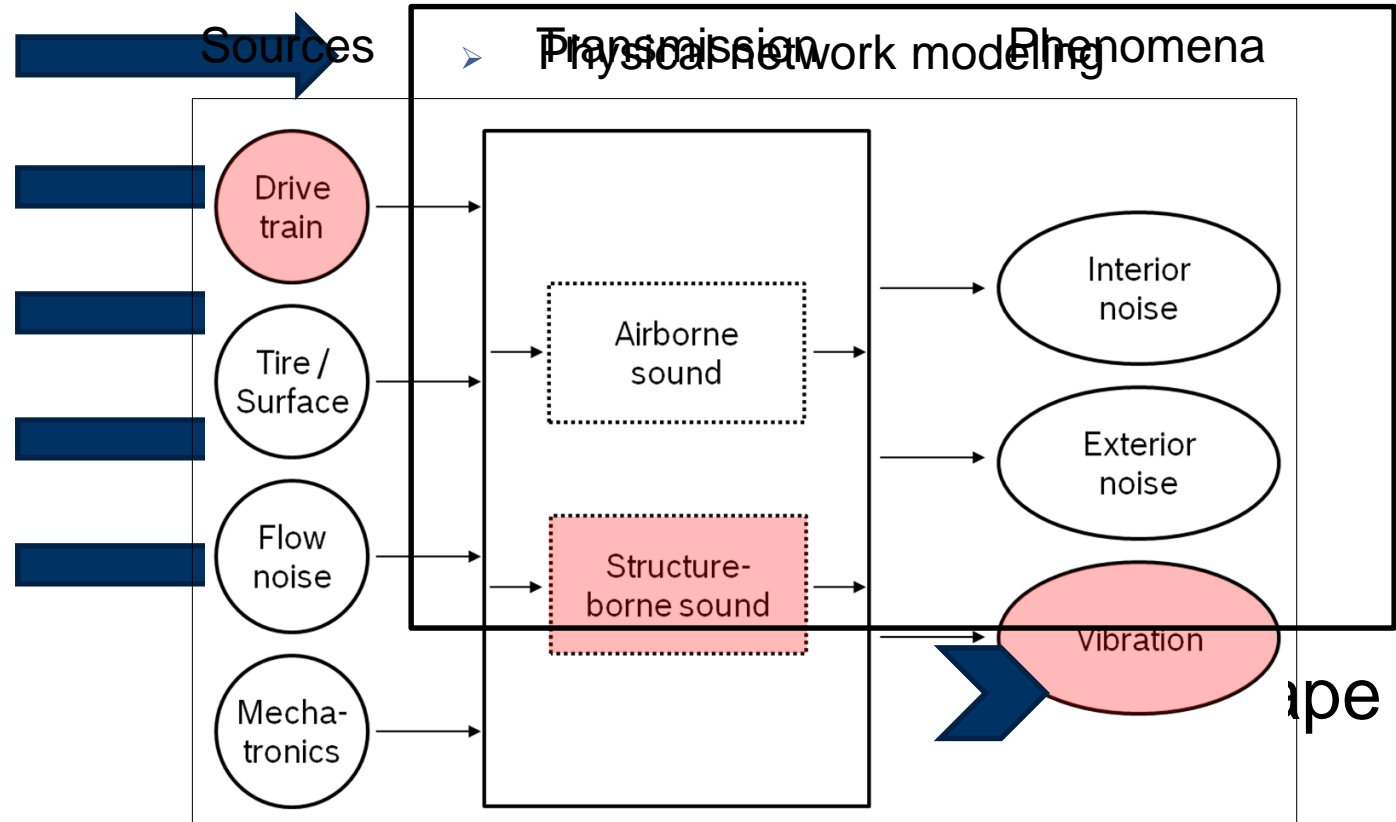
[1]

## Vibro-acoustic sources and transmission paths



## Requirements for a vibro-acoustic gear model

- Multidomain simulation
- Simple model usage
- Model extension
- Efficient simulation
- Three-dimensional gear mesh excitation

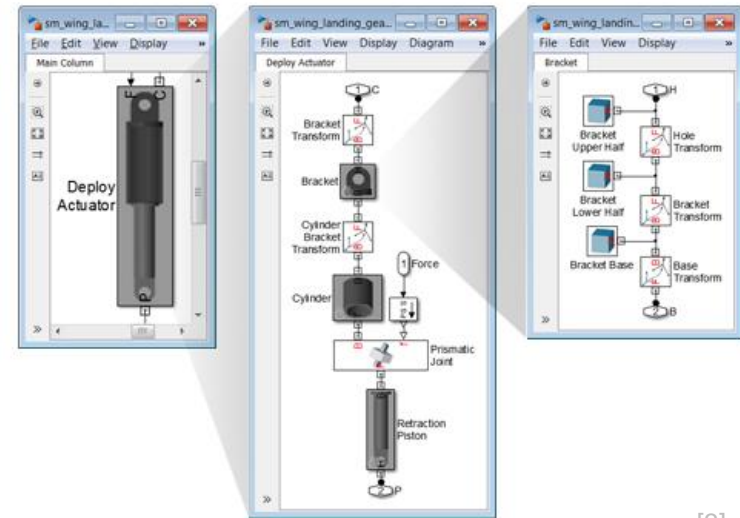
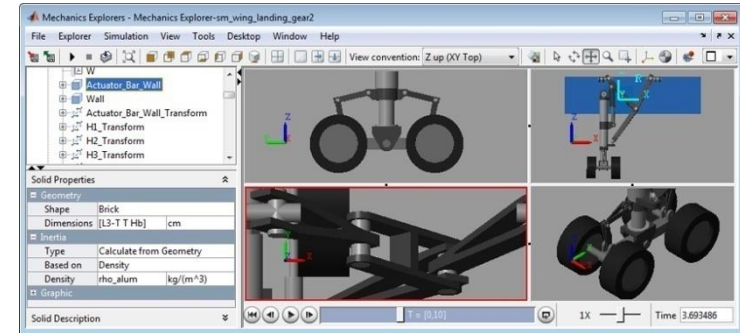


[2]

## SimMechanics™



- Multibody simulation environment
- 3D mechanical systems
- Cross-domain simulation
- Visualization and animation
- Interfaces to CAD-software



[3]





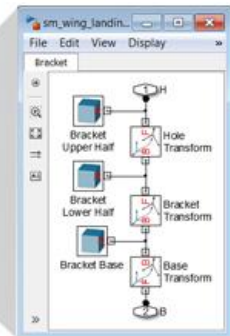
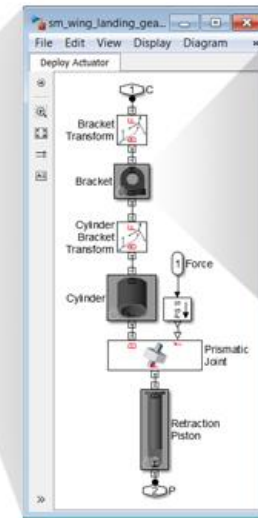
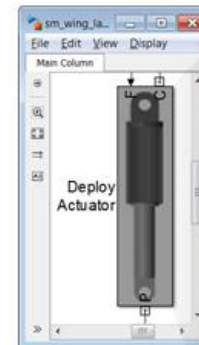
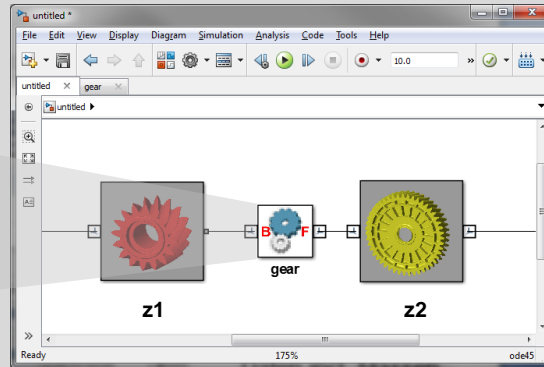
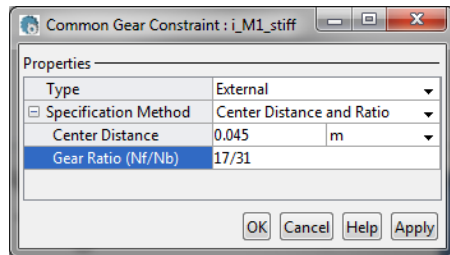
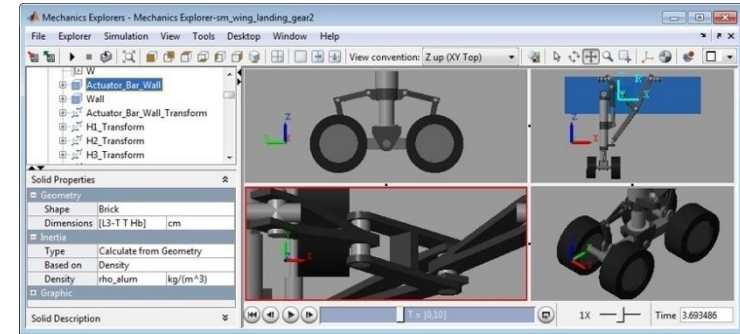
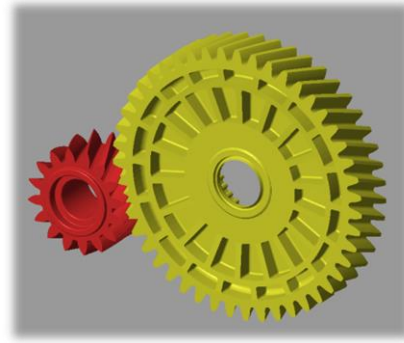
## SimMechanics™ — Common Gear Constraint



### Common Gear Constraint

$$\varphi_1 \cdot r_1 + \varphi_2 \cdot r_2 = 0$$

Need for an advanced gear model!

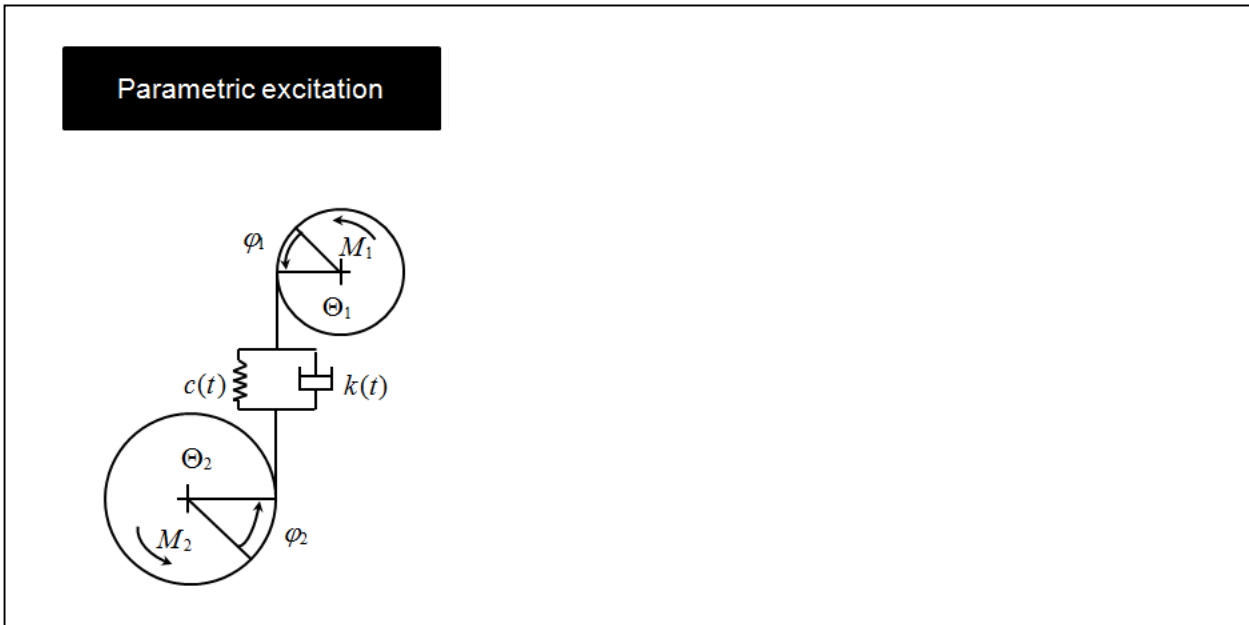


[3]



## Vibro-acoustic sources within a gear

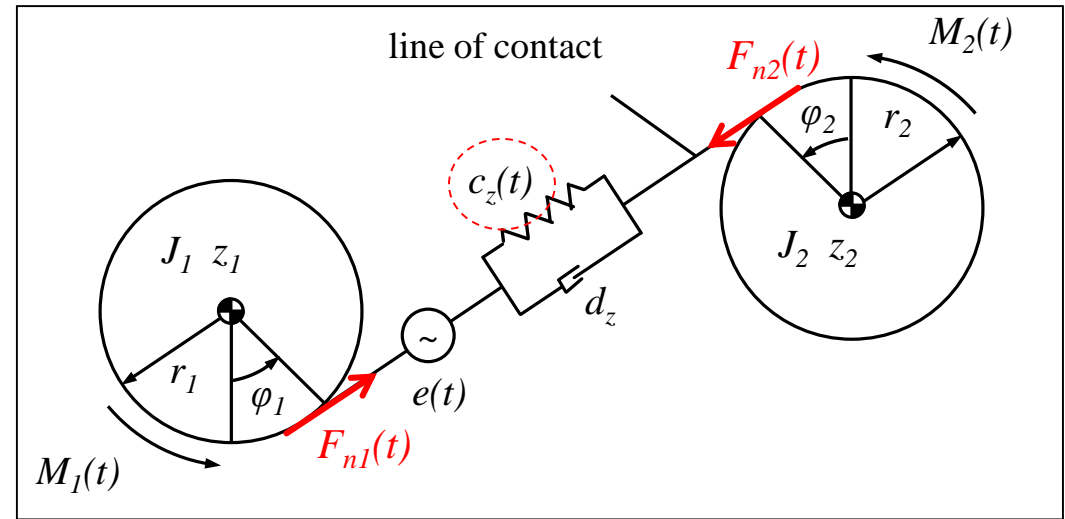
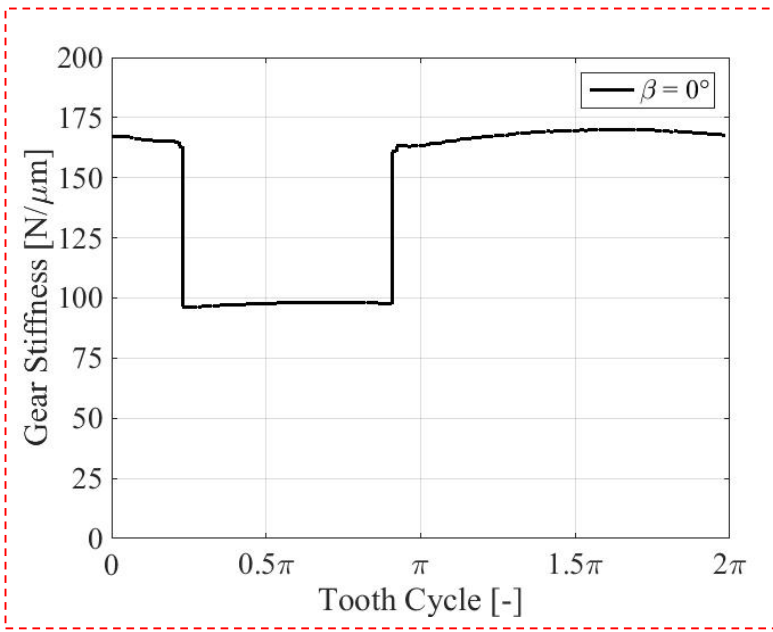
### Mechanical excitation mechanisms



[4]

- Parametric excitation
- Geometric excitation
- Impulse excitation

## Mathematical characterization of a lumped parameter gear model



[5]

## Formulation of a dynamic mathematical gear model

## Mathematical characterization of a LPM gear model

$F_t$ : Tangential force

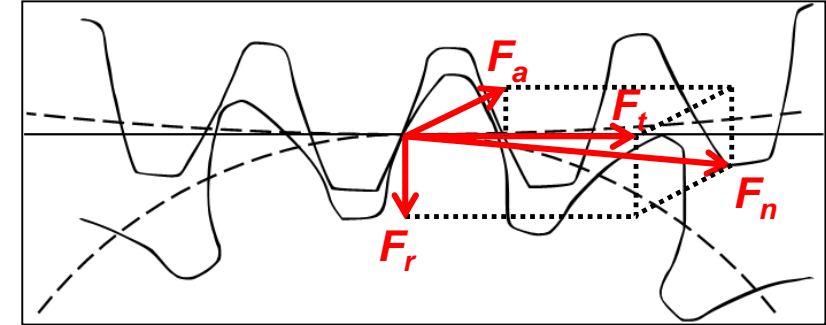
$\alpha_n$ : Normal pressure angle

$F_r$ : Radial force

$\beta$ : Helix angle

$F_a$ : Axial force

$F_n$ : Tooth normal force



[5]

### Calculation

$$M_1 = F_t \cdot r_1 \quad (1)$$

$$F_t = F_n \cdot \cos(\beta) \cdot \cos(\alpha_n) \quad (2)$$

(1) and (2):

$$F_n = \frac{M_1}{r_1 \cdot \cos(\beta) \cdot \cos(\alpha_n)}$$

$$\begin{bmatrix} F_t \\ F_r \\ F_a \end{bmatrix} = A_\beta A_{\alpha_n} \begin{bmatrix} F_n \\ 0 \\ 0 \end{bmatrix}$$



### Rotational matrixes

$$A_\beta = \begin{pmatrix} \cos \beta & 0 & -\sin \beta \\ 0 & 1 & 0 \\ \sin \beta & 0 & \cos \beta \end{pmatrix}$$

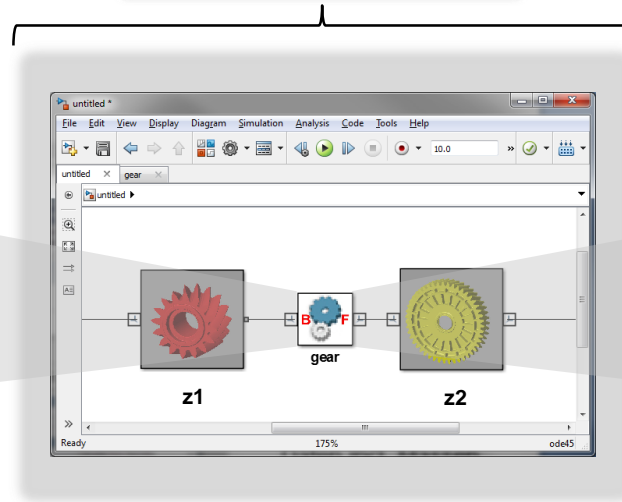
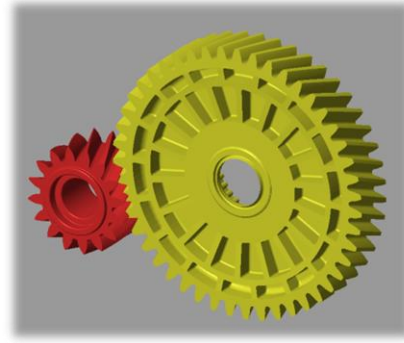
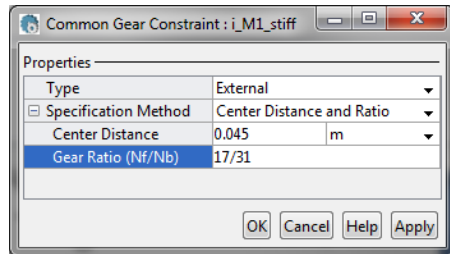
$$A_{\alpha_n} = \begin{pmatrix} \cos \alpha_n & -\sin \alpha_n & 0 \\ \sin \alpha_n & \cos \alpha_n & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

## SimMechanics™ - Common Gear Constraint

### Common Gear Constraint

$$\varphi_1 \cdot r_1 + \varphi_2 \cdot r_2 = 0$$

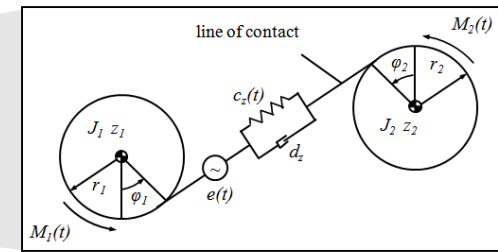
Kinematic constraint



### Flexible Gear Model

$$\varphi_1 \cdot r_1 + \varphi_2 \cdot r_2 \neq \text{TE} \quad \text{e.g. [6,7]}$$

Additional degree of freedom



Library extension enables transmission error (TE) and gear force calculation

## SimMechanics™ - Flexible Gear Model

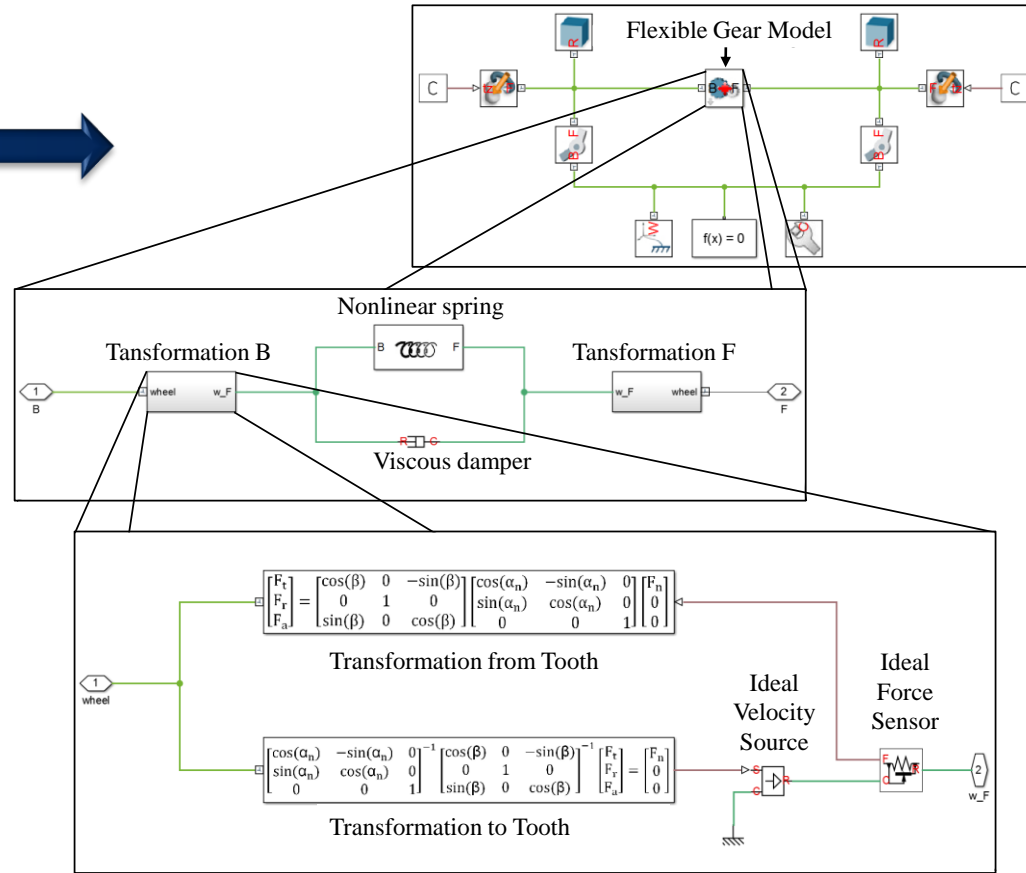
System level



Coupling layer



Transformation



[5]

## SimMechanics™ - Flexible Gear Model

**Block Parameters: Flexible Gear Model**

Subsystem (mask)

Parameters

Tooth Stiffness [N/m]  
gear\_compliance

Tooth Damping [N/(m/s)]  
1e2

Normal Module [m]  
0.0015

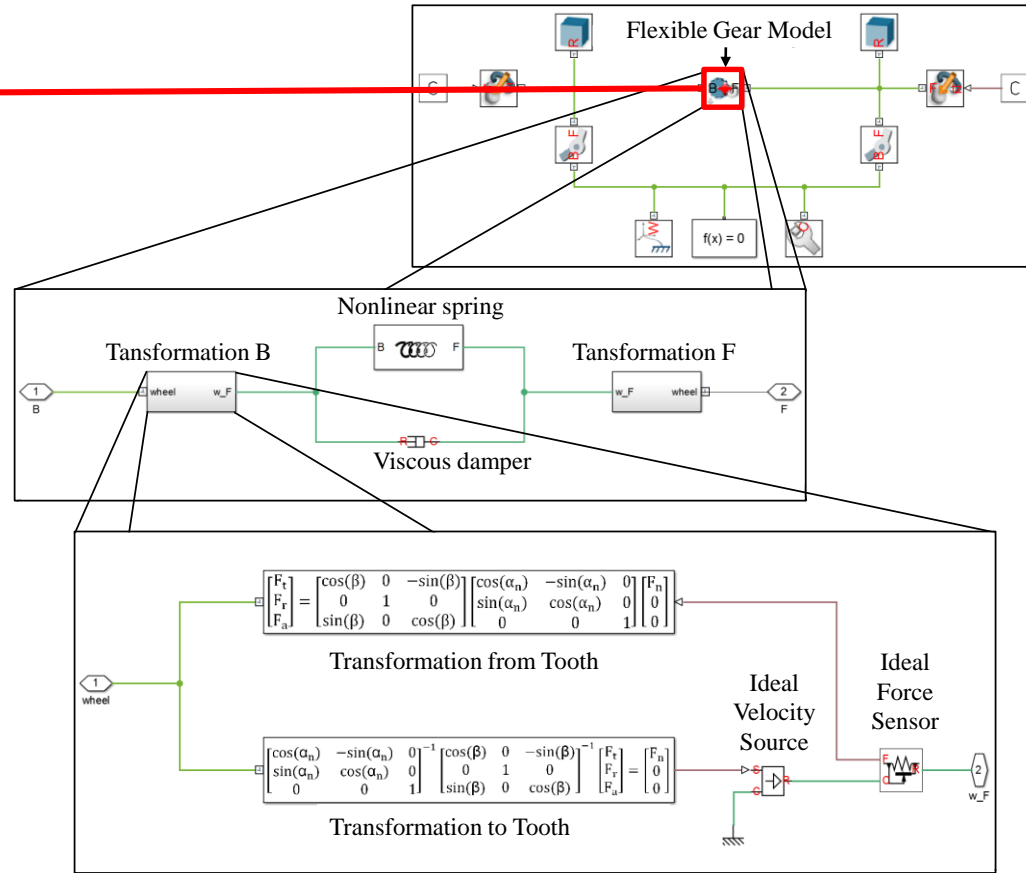
Tooth Number of B [-]  
19

Tooth Number of F [-]  
31

Normal Pressure Angle [rad]  
20/180\*pi

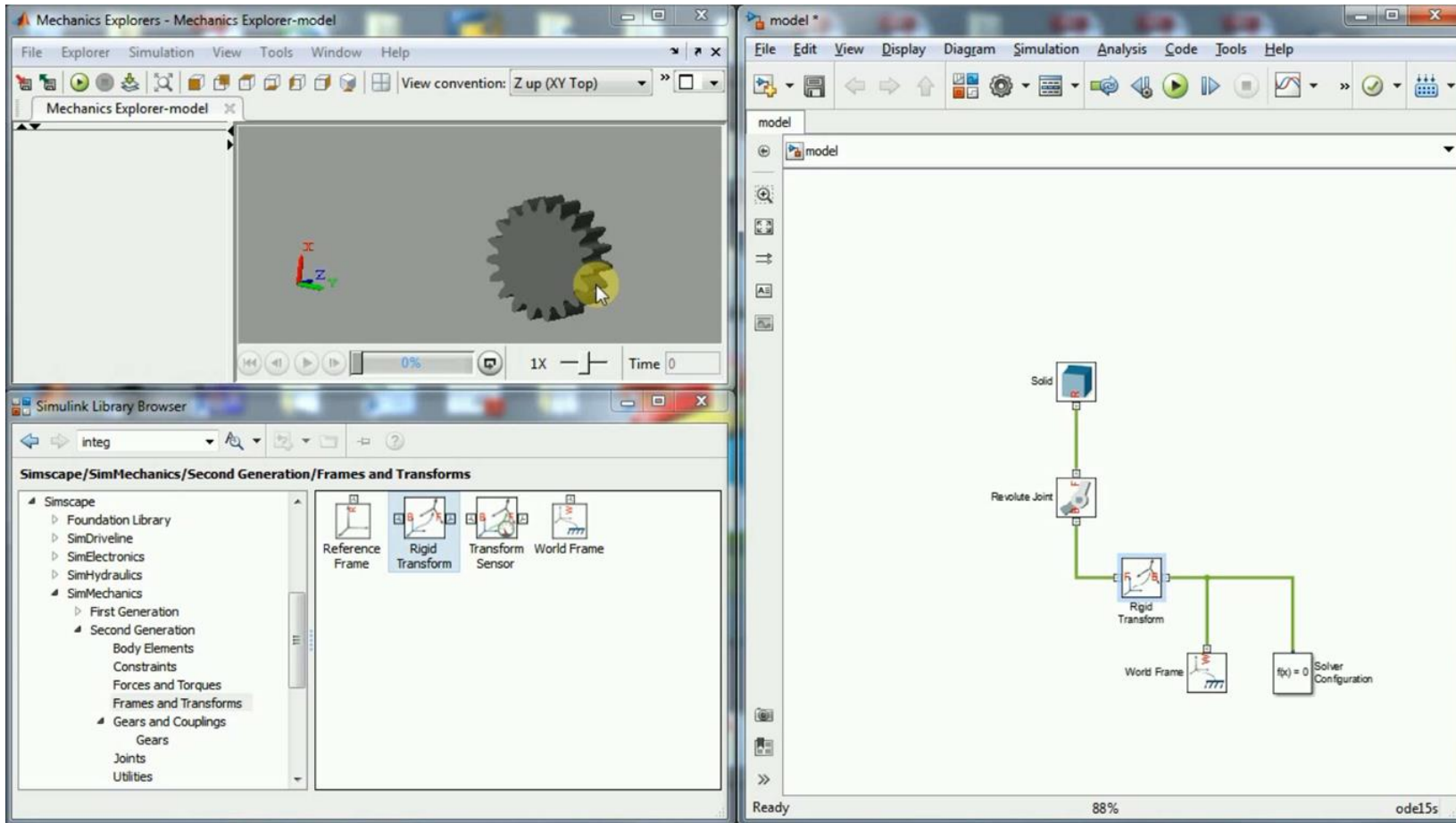
Helix Angle [rad]  
0

OK Cancel Help Apply



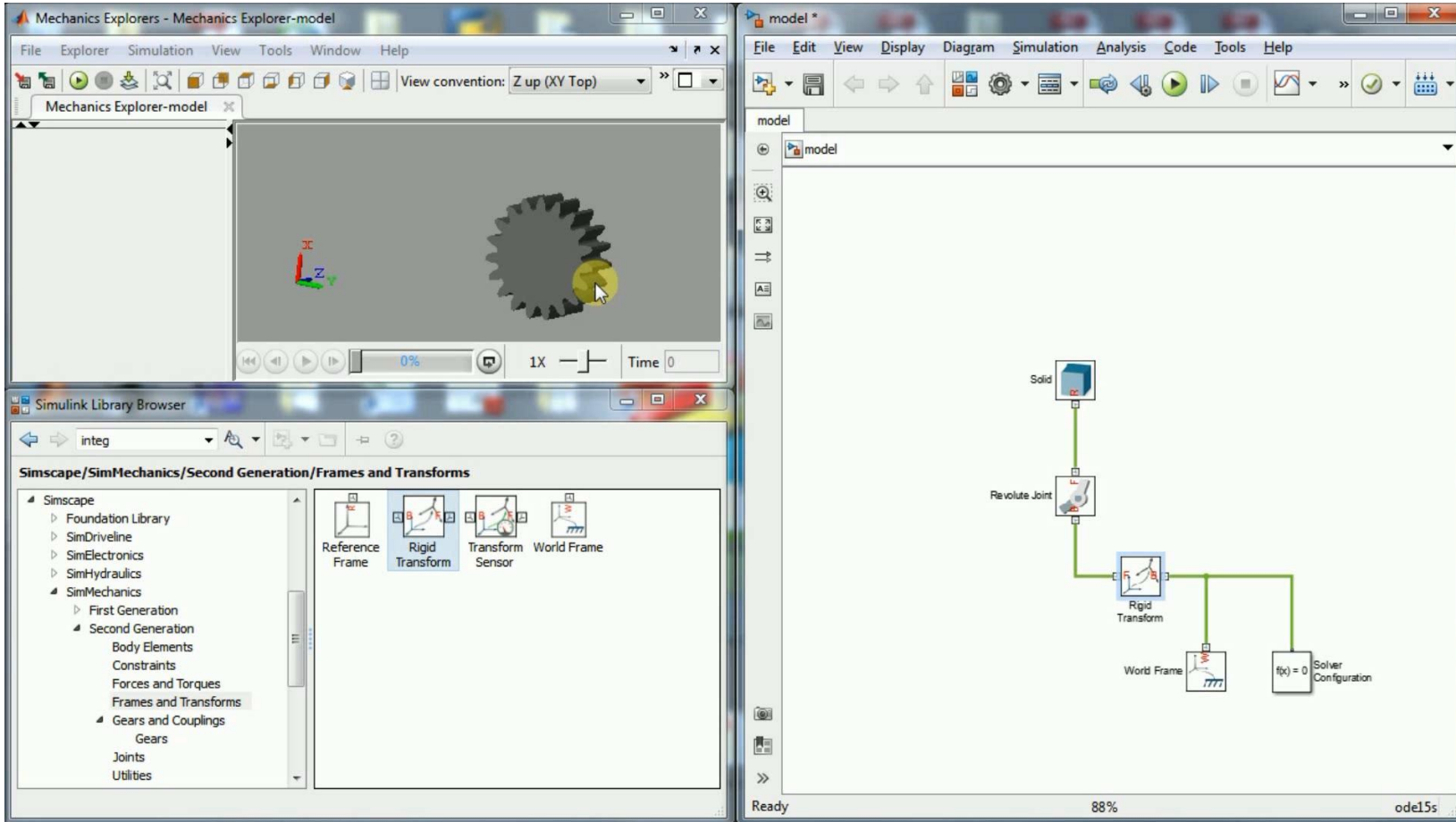
[5]

## SimMechanics™ - Flexible Gear Model

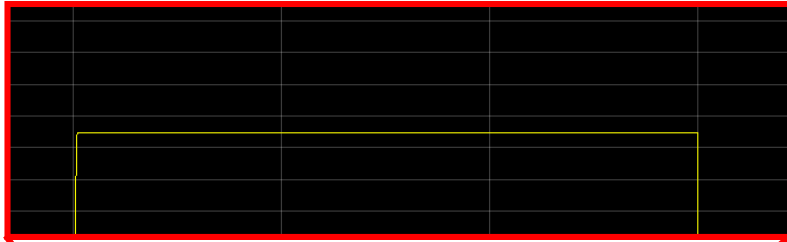




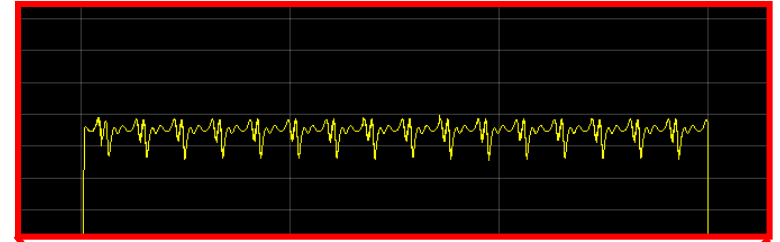
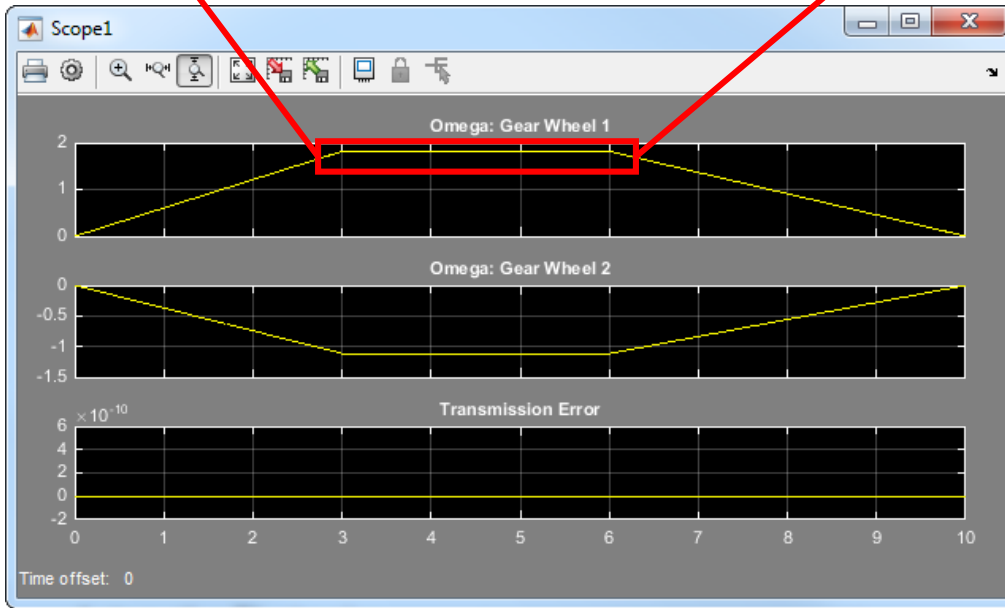
## SimMechanics™ - Flexible Gear Model



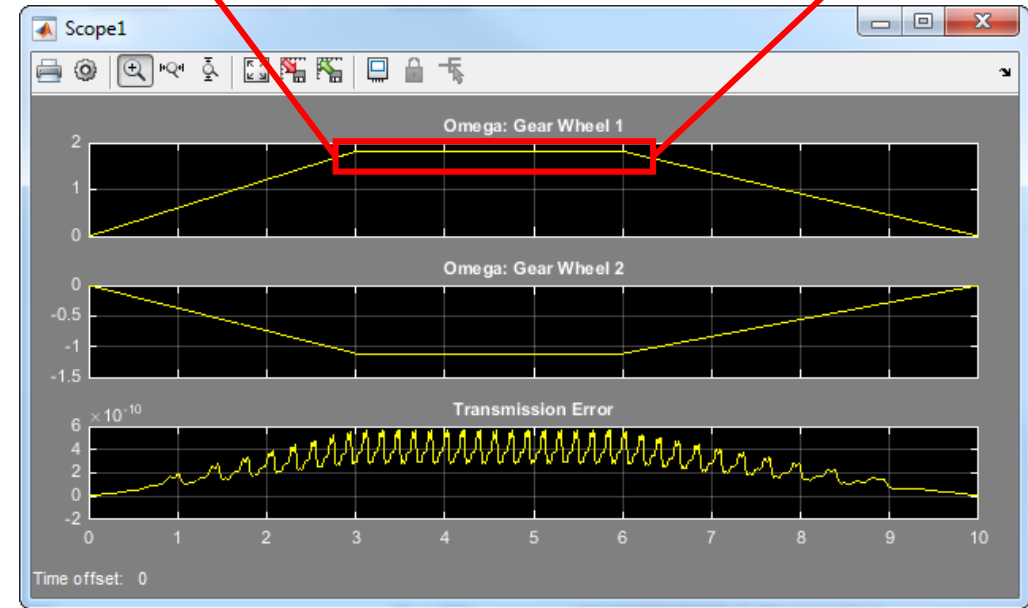
# SimMechanics™ - Flexible Gear Model - Analysis



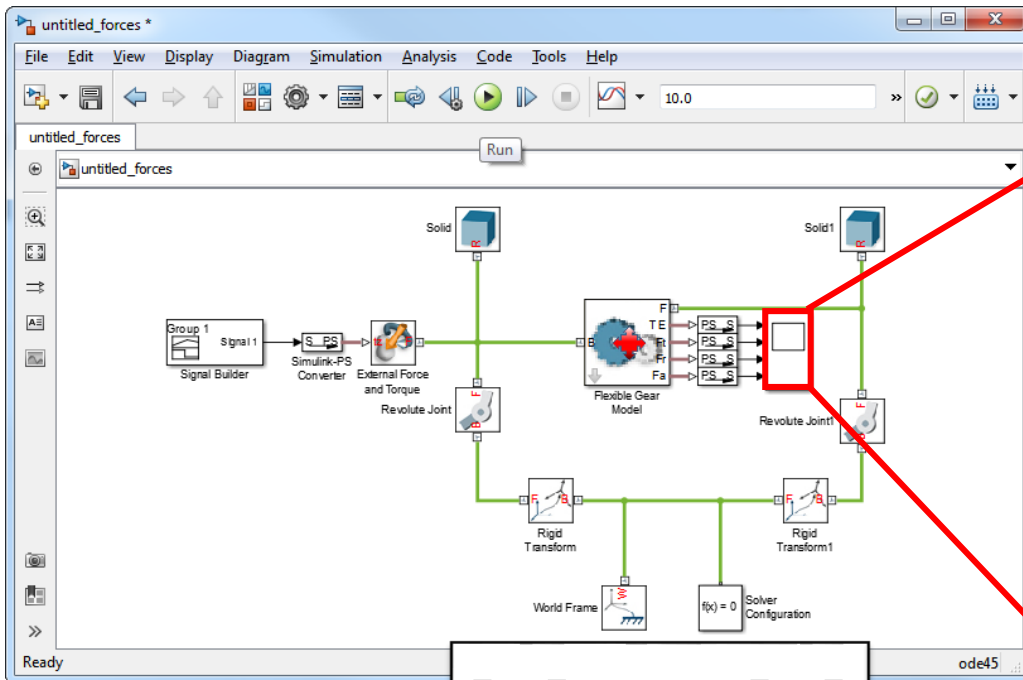
Common Gear Constraint



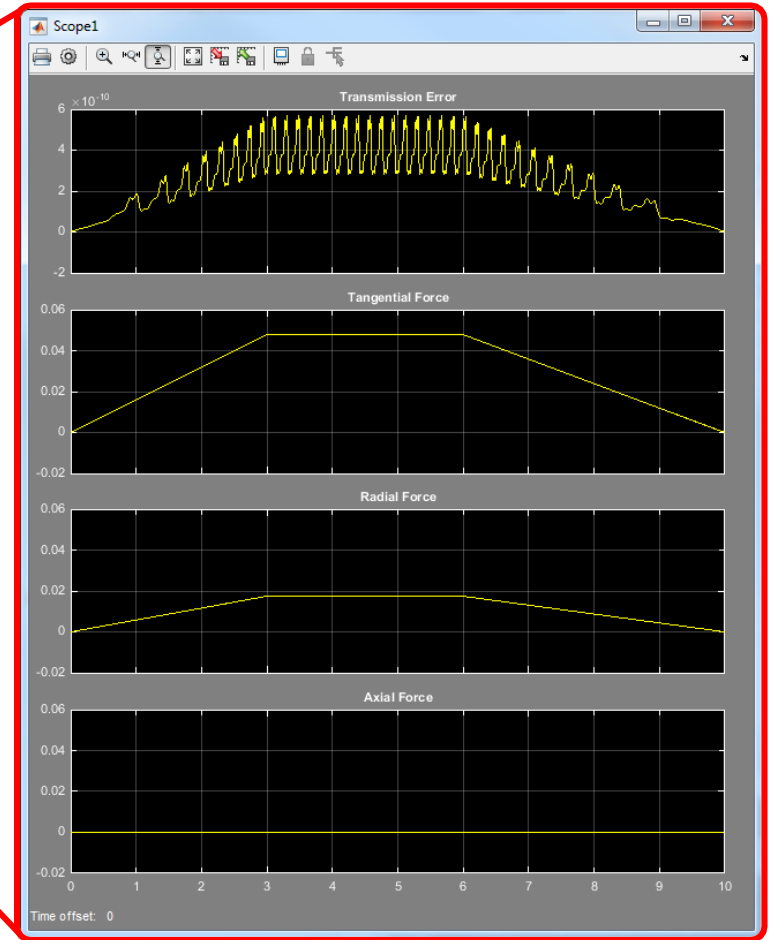
Flexible Gear Model



## SimMechanics™ - Flexible Gear Model - Analysis

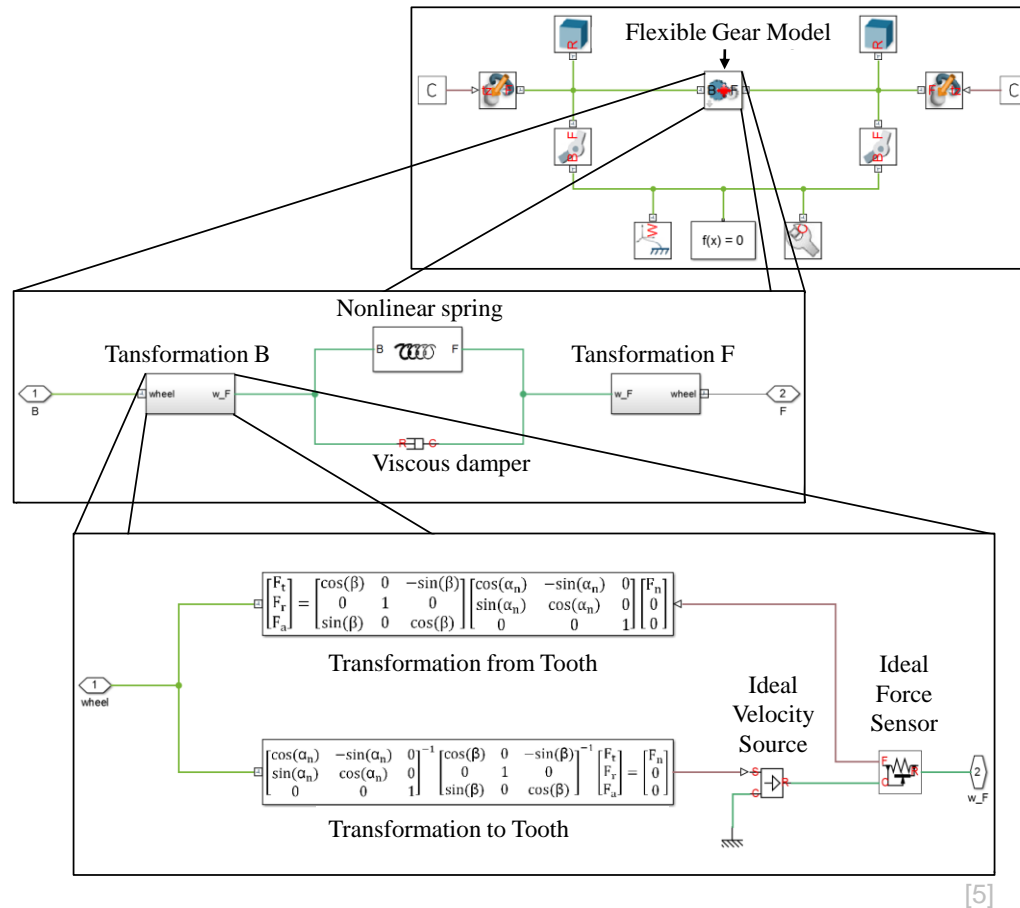


$$\begin{bmatrix} F_t \\ F_r \\ F_a \end{bmatrix} = A_\beta A_{\alpha_n} \begin{bmatrix} F_n \\ 0 \\ 0 \end{bmatrix}$$



## Conclusions

- Implementation of a modular flexible gear model
- Three-dimensional gear mesh excitation
- Calculation of TE
- Calculation of gear forces



[5]

## Further information regarding gear modeling

### **Flexible Gear Model Library - Vibration Excitation Mechanisms and Gear Force Calculation**

T. Dackermann, S. Miller, L. Hedrich, Rolando Doelling, Modelling, Identification and Control, Computational Intelligence, MIC, 826-010, Innsbruck, February 2015

- More details concerning the Simscape gear library
- Some results of verification

### **Method for system level vibro-acoustic gear modeling and simulation of electro-mechanical drive trains**

T. Dackermann, Rolando Doelling, L. Hedrich, IEEE International Symposium on Systems Engineering (ISSE), Rom, September 2015

- Heterogeneous system modeling and vibro-acoustic gear simulation
- Flexible housing and airborne sound emission
- Validation of model by means of measurements

## Images and literature sources

- [1] Bosch GmbH, <http://www.bosch.com>
- [2] P. Zeller, *Handbuch Fahrzeugakustik: Grundlagen, Auslegung, Berechnung, Versuch* (ATZ/MTZ-Fachbuch) Gebundene Ausgabe – 14. Mai 2009
- [3] MathWorks, <http://www.mathworks.com/>
- [4] A. Gacka, *Entwicklung einer Methode zur Abbildung der dynamischen Zahneingriffsverhältnisse von Stirn- und Kegelradsätzen*, Bericht aus der Produktionstechnik, Shaker Verlag, 2013
- [5] T. Dackermann, S. Miller, L. Hedrich, Rolando Doelling, *Flexible Gear Model Library - Vibration Excitation Mechanisms and Gear Force Calculation*, Modelling, Identification and Control, Computational Intelligence, MIC, 826-010, Innsbruck, February 2015
- [6] M. Henriksson, *On noise generation and dynamic transmission error of gears*, ISBN 978-91-7415-537-2, Stockholm 2009
- [7] D. R. Housser et al., *Comparison of transmission error predictions with noise measurements for several spur and helical gears*. National Aeronautics and Space Administration, 1994.